

Math 308 Discussion Problems  
Spring 2017

8. Find an *invertible*  $n \times n$  matrix  $A$  and an  $n \times n$  matrix  $B$  such that  $\text{rank}(AB) \neq \text{rank}(BA)$ , or explain why such matrices cannot exist.

9. Find a  $3 \times 4$  matrix  $A$  with nullity 2 and with

$$\text{col}(A) = \text{span} \left\{ \begin{bmatrix} 1 \\ 0 \\ 1 \end{bmatrix}, \begin{bmatrix} 4 \\ -3 \\ 7 \end{bmatrix}, \begin{bmatrix} 3 \\ -2 \\ 5 \end{bmatrix} \right\},$$

or explain why such a matrix can't exist.