1. Compute the convolution of $e^{-2 t}$ and $e^{-3 t}$.
2. Compute the convolution of $e^{a t}$ and $e^{b t}$ for any nonzero constants $a$ and $b$.
3. Compute the convolution of $e^{-t}$ and 1 .
4. Compute the convolution of $e^{-t}$ and $t$.
5. Compute the convolution of $e^{-t}$ and $t^{2}$.
6. Compute the convolution of $e^{-t}$ and $\cos t$.
7. Compute the convolution of $e^{-t}$ and $\sin t$.
8. Compute the convolution of $\cos 2 t$ and $\sin t$.
9. Compute the convolution of $\cos 2 t$ and $\sin 2 t$.
10. Use the techniques from class $(e(t)$, etc.) to solve these initial value problems:
(a) $y^{\prime \prime}+y=g(t), y(0)=1, y^{\prime}(0)=0$
(b) $y^{\prime \prime}-5 y^{\prime}+4 y=g(t), y(0)=1, y^{\prime}(0)=-1$
(c) $y^{\prime \prime}+4 y^{\prime}+3 y=g(t), y(0)=-2, y^{\prime}(0)=3$
(d) $y^{\prime \prime}+2 y^{\prime}+2 y=g(t), y(0)=1, y^{\prime}(0)=-2$
