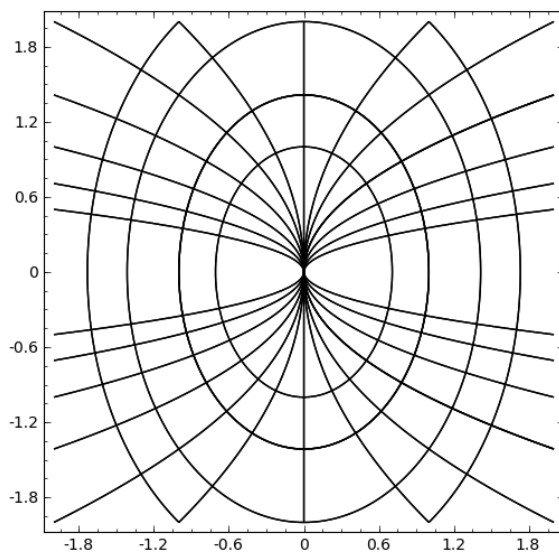


Math 134: Homework 4  
Due October 21

1. Two curves are called *orthogonal* if, wherever they intersect, they intersect at a right angle. (That is, their tangent lines are perpendicular at each point of intersection.) Two families of curves are *orthogonal trajectories* if each curve from one family is orthogonal to each curve from the other family.

Show that the family of parabolas  $x = ay^2$  and the family of ellipses  $x^2 + \frac{1}{2}y^2 = b$  (for all real numbers  $a$  and all positive real numbers  $b$ ) are orthogonal trajectories.



2. Let  $f$  be a function that is differentiable for all  $x \geq 0$ . Suppose that  $f'(x)$  satisfies the condition

$$a \leq f'(x) \leq b \text{ for all } x > 0.$$

Show that for all  $x > 0$ ,

$$f(0) + ax \leq f(x) \leq f(0) + bx.$$

(Hint: use the Mean Value Theorem.)