Math 134: Homework 9 Due December November 3

(1) By the Fundamental Theorem of Calculus, if f has a continuous first derivative on the interval [a, b] then

$$f(b) = f(a) + \int_{a}^{b} f'(x) \, dx$$
.

(a) Assume that f has a continuous second derivative on [a, b], and apply integration by parts to the integral above to derive the identity

$$f(b) = f(a) + f'(a)(b-a) - \int_a^b f''(x)(x-b) \, dx \, .$$

(b) Finally assume that f has a continuous third derivative on [a, b] and apply integration by parts once more to derive the identity

$$f(b) = f(a) + f'(a)(b-a) + \frac{f''(a)}{2}(b-a)^2 + \frac{1}{2}\int_a^b f'''(x)(x-b)^2 \, dx \, .$$

(2) Evaluate the integral
$$\int \frac{x^2}{(x^2+4x+5)^{3/2}} dx.$$

(3) Evaluate the integral
$$\int \frac{4 \arctan x}{(x+1)^3} dx.$$