

Some Laplace transforms

Definition of Laplace transform: $\mathcal{L}(f(t)) = \int_0^\infty e^{-st} f(t) dt$

$f(t)$	$F(s)$
0	0
1	$\frac{1}{s}, \quad s > 0$
e^{at}	$\frac{1}{s-a}, \quad s > a$
$t^n, \quad n = 1, 2, 3, \dots$	$\frac{n!}{s^{n+1}}, \quad s > 0$
$\sin(at)$	$\frac{a}{s^2 + a^2}, \quad s > 0$
$\cos(at)$	$\frac{s}{s^2 + a^2}, \quad s > 0$
$e^{at} \sin(bt)$	$\frac{b}{(s-a)^2 + b^2}, \quad s > a$
$e^{at} \cos(bt)$	$\frac{s-a}{(s-a)^2 + b^2}, \quad s > a$
$e^{ct} f(t)$	$F(s-c)$
$f'(t)$	$sF(s) - f(0)$
$f''(t)$	$s^2F(s) - sf(0) - f'(0)$
$f^{(n)}(t)$	$s^nF(s) - s^{n-1}f(0) - \dots - f^{(n-1)}(0)$
$u_c(t)$	$e^{-cs} \frac{1}{s}$
$u_c(t) f(t-c)$	$e^{-cs} F(s)$
$\delta(t-c)$	e^{-cs}
<div style="display: flex; justify-content: space-between;"> <div style="width: 45%;">t^p</div> <div style="width: 45%;">$\frac{\Gamma(p+1)}{s^{p+1}}, \quad s > 0$</div> </div> <p style="text-align: center; margin: 5px 0;">(where $\Gamma(p+1) = \int_0^\infty e^{-x} x^p dx$)</p> <div style="display: flex; justify-content: space-between;"> <div style="width: 45%;">$\int_0^t f(t-u)g(u)du$</div> <div style="width: 45%;">$F(s)G(s)$</div> </div>	