Math 308: Linear Algebra

A List of Topics for the First Midterm

Here's a list of things you should be comfortable doing for the exam.

1. Linear Systems of Equations (Section 1.1)

- (a) Solve a linear system of equations in echelon form.
- (b) Tell when a linear system has zero, one, or infinitely many solutions.

2. Elimination and augmented matrices (Section 1.2)

- (a) Write a linear system of equations as an augmented matrix.
- (b) Perform Gaussian elimination to write a matrix in echelon form.
- (c) Perform Gauss-Jordan elimination to write a matrix in reduced echelon form.
- (d) Interpret the form of a reduced matrix to determine when the corresponding linear system has 0, 1, or infinitely many solutions.

3. Applications of linear systems (Section 1.4)

- (a) Solve traffic flow problems and balance chemical equations.
- (b) Use linear systems of equations to answer Math 126-style questions about lines and planes.

4. Vectors (Section 2.1)

- (a) Do addition and scalar multiplication of vectors algebraically and geometrically.
- (b) Write one vector as a linear combination of other vectors, or tell when you can't.

5. Span (Section 2.2)

- (a) Tell when a set of vectors spans \mathbb{R}^n , and when some vector is in the span of another set of vectors.
- (b) Multiply a matrix by a vector, and understand what this means about the span of the column vectors of that matrix.

6. Linear independence (Section 2.3)

- (a) Tell when some set of vectors is linearly independent.
- (b) Know how span, linear independence, and matrix multiplication interact, especially in the case of n vectors in \mathbb{R}^n (see the "big theorem").

7. Linear transformations (Section 3.1)

- (a) Tell when a transformation is linear.
- (b) Write a linear transformation in the form $T(\mathbf{x}) = A\mathbf{x}$ for some matrix A.
- (c) Interpret linear transformations graphically.
- (d) Check whether a linear transformation is onto, or whether some vector is in the range of that linear transformation. In particular, know how these relate to the column vectors of the matrix A.
- (e) In the case of linear transformations from \mathbb{R}^n to \mathbb{R}^n , apply the big theorem to relate whether T is one-to-one and whether it's onto.