

Math 125 H - Winter 2015
Midterm Exam Number Two
February 26, 2015

Name: _____

Student ID no. : _____

Signature: _____

Section: _____

1	14	
2	14	
3	8	
4	6	
5	12	
6	6	
Total	60	

θ	$\sin(\theta)$	$\cos(\theta)$	$\tan(\theta)$
0	0	1	0
$\pi/6$	1/2	$\sqrt{3}/2$	$1/\sqrt{3}$
$\pi/4$	$\sqrt{2}/2$	$\sqrt{2}/2$	1
$\pi/3$	$\sqrt{3}/2$	1/2	$\sqrt{3}$
$\pi/2$	1	0	-

- The exam consists of SIX problems on SIX pages, including this cover sheet.
- Show all work for full credit.
- You do not need to simplify your answers.
- If you use a trial-and-error or guess-and-check method when a more rigorous method is available, you will not receive full credit.
- If you write on the back of the page, please indicate that you have done so!
- You may use one hand-written double-sided 8.5" by 11" page of notes.
- You have 80 minutes to complete the exam.

1. [7 points per part] Here are a bunch of integrals. Evaluate them.

(a) $\int 3 \sin^4(x) \cos^5(x) dx.$

(b) $\int \sin(2x)e^{3x} dx$

2. [7 points per part] Good news! We haven't run out of integrals yet.

(a) $\int_2^3 \frac{2x^2 + 9x - 3}{x^3 - x^2 + x - 1} dx$

(b) $\int_{-1}^0 \frac{x}{(-x^2 - 2x + 3)^{5/2}} dx$

3. **[8 points]** Let $f(x)$ be a function such that $f(x) > 0$ on the interval $(0, \infty)$, and $f(x)$ is continuous on the interval $[0, \infty)$.

Let \mathcal{R} be the region in the first quadrant bounded by $y = f(x)$, $x = 0$, and $x = a$.

Let \mathcal{S}_x be the solid formed by revolving \mathcal{R} around the x -axis, and let \mathcal{S}_y be the solid formed by revolving \mathcal{R} around the y -axis.

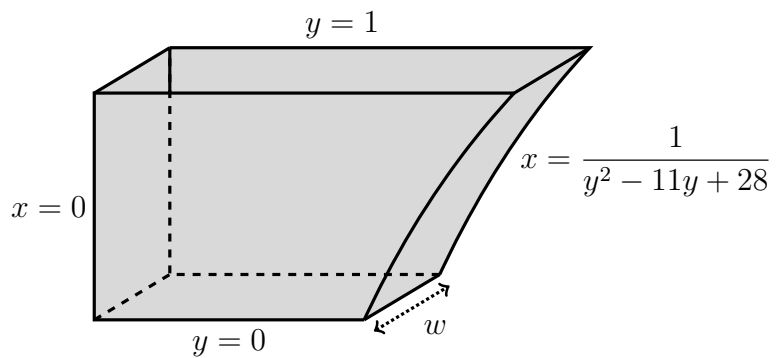
Find a function $f(x)$ such that for **all** $a > 0$, the solids \mathcal{S}_x and \mathcal{S}_y are equal in volume.

4. **[6 points]** Use Simpson's Rule with $n = 6$ to estimate the average value of $f(x) = 2^{(x^2-3)}$ on the interval $[-4, 8]$. You do not need to simplify your answer!

5. [12 points] The front of an aquarium tank is shaped like the region in the first quadrant bounded by $y = 1$ and $x = \frac{1}{y^2 - 11y + 28}$.

The aquarium itself is a prism, and the two bases are w meters apart.

The tank is filled with a liquid of density D . Let g be the acceleration due to gravity.



Compute the work needed to empty the tank by pushing all the liquid to the very top.
(Your answer will include w , D , and g .)

6. [6 points] Does the integral $\int_0^{\infty} \frac{\sin^2(x)}{x^2 + \sqrt{x}} dx$ converge or diverge? Explain.

I feel like you probably don't need a whole page for that problem, so here's a Sudoku. Boxes with slashes contain two digits, with the lower number on top.

/	3	5	1/	/9	
/		/			/
/	7	/9			/5
8	/		2/	/4	
	/			/	/
	/2	/4	/6	8	