MIDTERM #1

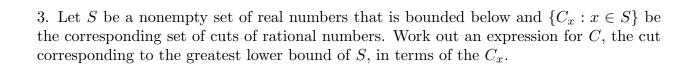
Math 327C

name

Show all work; doing this may help you get more partial credit for problems done incorrectly. Use the backs of the test pages as necessary.

1. Show carefully, using the definition of limit, that $\frac{4}{7n^2+3} \to 0$ as $n \to \infty$.

- 2. The following are *incorrect* versions of theorems proved in class. In each case give the *correct* statement of the theorem.
- (a) A bounded sequence converges if and only if it is monotone.
- (b) Every nonempty set of real numbers that is bounded below has a least lower bound.
- (c) There are no subsets of \mathbb{R} that are both closed and open.



4. Show that $\sum_{i=1}^{\infty} \frac{\sin^2 i}{2^i}$ converges, by showing that its partial sums are bounded.

5. Decide whether the series $\sum_{n=1}^{\infty} \frac{5n+4}{n^3+7}$, converges, making sure to state explicitly which test you are using.