Holly Jolly Auction

1. Write the number 200 as the sum of as many distinct primes as possible. For example, 200 = 97 + 103 is a valid answer, but not a very good one because you only used 2 primes.

2. An integer's abundance ratio is the ratio of the sum of its divisors to itself. For example, 36 has factors

The sum of the factors of 36 is 91. So the abundance ratio of 36 is $91/36 \approx 2.528$. Find a number, not containing the digit 0, less than $1\,000\,000$, with the largest abundance ratio.

3. You have 8 pancakes in a stack, one with one blueberry, one with two blueberries, one with three blueberries, and so on. Count the number of blueberries in the top pancake and call that number N. Pick up the stack of the top N pancakes and flip it upside down. Repeat this procedure until the pancake with one blueberry ends up on the top. Find an initial arrangement of pancakes that takes the largest number of flips for the pancake with one blueberry to end up on the top.

4. For a pair of words of the same length, we can calculate their partner score as follows. The pair gets 1 point for each letter they have in common in a different position within each word. For example, the pair "OPENS" and "CLOSE" has a partner score of 3, and the pair "JUMP" and "PUMA" has a partner score of 1. Find a pair with the largest partner score possible.

5. Four positive integers less than 100 are written at the corners of a large square. Every minute, four dots are drawn at the midpoints of the square's edges, and labeled with the positive difference between the adjacent numbers. These midpoints are connected to form a new square, and then the process repeats. This continues until we form a square whose corners are all labeled 0. Find initial labels of the square that take the most steps for this to occur.