## UW Math Circle Worksheet

1.	Harad has $n$ towns and $n-2$ roads between towns. Show that you cannot travel from any town to any other town through a sequence of roads.
2.	In Beleriand, there are $2n$ villages and every village has roads to at least $n$ other villages. Show that you can travel from any village to any other village through a sequence of roads.
3.	In Gondor, there are $2n$ towns, every town has roads to at least $n-1$ towns, and the largest town has roads to at least $n$ towns. Show that you can travel from any town to any other town through a sequence of roads.
4.	A horde of orcs have attacked the town of Osgiliath in Gondor. Osgiliath no longer exists and all roads to Osgiliath no longer exist. Luckily, Osgiliath only had roads to $n-1$ other towns. Show that you still can travel from any town to any other town through a sequence of roads.