

Exam I Answers
Math 126 C Winter 2019

1. (1 point each)
 - (a) i. NONE; ii. $(0, \pm 1, 0)$; iii. $(0, 0, \pm 2)$
 - (b) i. ellipse; ii. hyperbola; iii. hyperbola
 - (c) hyperboloid of one sheet
2. (a)
 - i. (2 points) $a = 12, b = 0$
 - ii. (2 points) $\mathbf{proj}_{\mathbf{k}} \mathbf{n} = \langle 0, 0, -4 \rangle$
- (b) (3 points) $\theta = \cos^{-1} \left(\frac{1}{\sqrt{10}} \right)$
- (c) (3 points) Many possible correct answers. One is $x = \sin t, y = \cos t, z = 3 \sin t$
3. (2 points each) (a) T; (b) F; (c) T; (d) T; (e) F.
4. (7 points) Speed is $v(t) = \sqrt{4t^2 - 4t + 10}$, which is smallest when $4t^2 - 4t + 10$ is smallest. Use Calc I methods (or algebra) to find that smallest speed (occurring at $t = \frac{1}{2}$) is 3.
5. (8 points) $(\sqrt{6}, 2\sqrt{6}, 3 - \sqrt{6})$ and $(-\sqrt{6}, -2\sqrt{6}, 3 + \sqrt{6})$
6. (8 points) $r = \frac{1}{\kappa(\pi)} = \frac{(1 + \pi^2)^{3/2}}{2 + \pi^2}$