## Math 126 C - Spring 2010 Mid-Term Exam Number One April 20, 2010



| 1     | 10 |  |
|-------|----|--|
| 2     | 10 |  |
| 3     | 10 |  |
| 4     | 10 |  |
| 5     | 10 |  |
| Total | 50 |  |

- Complete all questions.
- You may use a scientific, non-graphing calculator during this examination. Other electronic devices are not allowed, and should be turned off for the duration of the exam.
- If you use a trial-and-error or guess-and-check method when an algebraic method is available, you will not receive full credit.
- You may use one hand-written 8.5 by 11 inch page of notes.
- Show all work for full credit.
- You have 50 minutes to complete the exam.

## 1. Determine whether or not the line

$$x = 4t - 7, y = 5t - 16, z = -2t + 14$$

and the line

$$x = t + 7, y = -3t - 7, z = 7t + 22$$

intersect. If they do, give the point of intersection.

2. Let *P* be the plane containing the points (1, 5, 2), (2, 3, 6) and (7, 4, 1). Find the intersection of *P* with the *y*-axis.

## 3. Consider the polar curve

 $r = \sin \theta \tan \theta.$ 

(a) Find an equivalent cartesian equation for this curve.

(b) The curve has a vertical asymptote. What is the equation of the asymptote?

- 4. Let *S* be the surface in 3D consisting of all points which are twice as far from the *z*-axis as they are from the *x*-axis.
  - (a) Give an example of a point on this surface, other than the origin.

(b) Give an equation for this surface.

(c) Describe this surface (if it is a quadric surface, categorizing it (i.e., ellipsoid, eliptic paraboloid, etc.) is sufficient).

5. Let P be the point in the first quadrant on the curve

$$x = \cos t, y = \csc t$$

such that the tangent line to the curve at *P* passes through the origin. Find the coordinates of *P*.

