

Your Name

Your Signature

Student ID #

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Your TA's name

Your Quiz Section Label and Time

Problem	Possible	Points
1	8	
2	10	
3	10	
4	12	
5	10	
Total	50	

- No books allowed. You may use a scientific calculator and one  $8\frac{1}{2} \times 11$  sheet of **handwritten** notes.
- Do not share notes.
- In order to receive credit, you must show your work and explain your reasoning (except on the “short answer” questions).
- Place a box around **YOUR FINAL ANSWER** to each question.
- If you need more room, use the backs of the pages and indicate to the grader where to find your work.
- Raise your hand if you have a question or need more paper.

Don't open the test until everyone has a copy and the start of the test is announced.

1 (8 points total) Recall that  $\vec{i}$ ,  $\vec{j}$ , and  $\vec{k}$  are the standard basis vectors. Give a **concrete** example of each of the following:

(a) (3 points) A **nonzero** vector  $\vec{v}$  such that  $\text{proj}_{\vec{k}} \vec{v} = \vec{0}$ .

(b) (5 points) A **unit** vector that is perpendicular to both  $\vec{i} + \vec{j}$  and  $\vec{j} - \vec{k}$ . How many different solutions are there?

2 (10 points) Consider the curve with the vector equation

$$\vec{r}(t) = \langle t, t^2 + 1, t^3 - 2t^2 \rangle$$

Is there a point on this curve where the tangent line is parallel to the vector  $\langle 10, 40, 40 \rangle$  ? If so, find the point. If not, explain why.

**3** (10 points total) Consider two planes given by the equations  $x+2y-3z = 5$  and  $2x-y+z = 0$ .

(a) (5 points) Find parametric equations of the line where the planes intersect.

(b) (5 points) Find the cosine of the angle between the planes.

4 (12 points total) Consider the curve given by the equation in polar coordinates

$$r = 2 \cos(\theta) + 4 \sin(\theta).$$

(a) (6 points) Find the Cartesian equation (non-parametric, in  $x$  and  $y$  coordinates) of the curve. Sketch the curve.

(b) (6 points) Find the equation of the tangent line to the curve at  $\theta = \pi/4$ .

**5** (10 points total) Consider the surface defined as the set of points which are equidistant from the  $x$ -axis and from the  $yz$ -plane.

(a) (6 points) Write down the equation of the surface.

(b) (4 points) Identify the surface.