

Your Name

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Your Signature

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Student ID #

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Quiz Section

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Professor's Name

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TA's Name

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- Turn off and stow away all cell phones, watches, pagers, music players, and other similar devices.
- This exam is closed book. You may use one  $8.5'' \times 11''$  sheet of handwritten notes (both sides OK). Do not share notes.
- You can use only a Texas Instruments TI-30X IIS calculator. No other models are allowed.
- In order to receive credit, you must **show all of your work**. If you do not indicate the way in which you solved a problem, or if the work shown is incorrect or incomplete, you may get little or no credit for it, even if your answer is correct.
- You may use directly the integral formulas # 1-18 in the table from section 7.5 of your textbook (posted on the departmental math 125 website), without deriving them. **Show your work in evaluating any other integrals, even if they are on your note sheet.**
- Place a box around your answer to each question. Unless otherwise instructed, simplify your answers, but leave them in exact form (for example  $\frac{\pi}{3}$  or  $5\sqrt{3}$ ).
- If you need more room, use the backs of the pages and indicate that you have done so.
- This exam has 8 pages, in addition to this cover sheet. Make sure you have a complete exam.

Question	Points	Score
1	14	
2	14	
3	10	
4	14	
5	14	

Question	Points	Score
6	10	
7	10	
8	14	
Total	100	

1. (14 points) Evaluate the following integrals. Show your work. Simplify and box your answers.

(a)  $\int \sqrt{x} \ln(\sqrt{x}) dx$

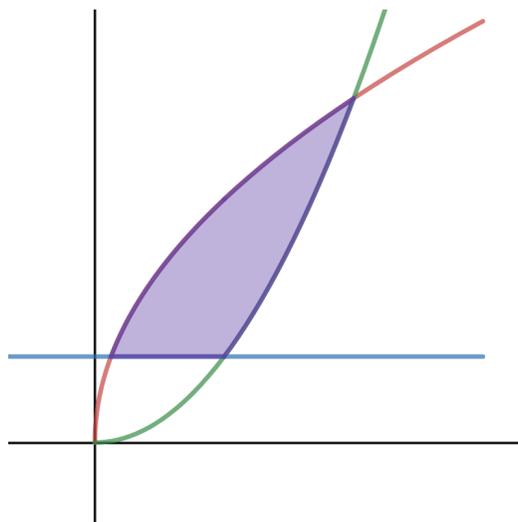
(b)  $\int \frac{1}{x^4 \sqrt{x^2 - 4}} dx$

2. (14 points) Evaluate the following integrals. Show your work. Simplify and box your answers.

(a)  $\int_0^{\pi/4} \frac{\sin^4 \theta}{\cos^6 \theta} d\theta$

(b)  $\int_0^{1/2} \frac{\sqrt{2x}}{2x-4} dx$

3. (10 points) Compute the area of the region that is bounded above by  $y = \sqrt{8x}$  and below by the line  $y = 1$  and the curve  $y = x^2$ . Simplify and box your answer.



4. (14 points) One model for air resistance predicts that a particular ball thrown straight up in the air will have velocity at  $t$  seconds given by:

$$v(t) = ce^{-t} - 10 \text{ meters/sec, for some constant } c,$$

where upward is considered positive velocity. Assume the ball is thrown straight upward starting from the ground with an initial velocity of 20 m/s.

- (a) Find the formula for the height  $h(t)$  of the ball after  $t$  seconds.
- (b) Find the **total distance** traveled by the ball from  $t = 0$  to  $t = 2$  seconds. You may give your final answer as a decimal accurate to 3 digits after the decimal point (or leave in exact form).

5. (14 points) A particle is sliding down the curve  $y = 10 - x^3$ . At time  $t = 0$  the particle starts at  $(0, 10)$ . The  $x$ -coordinate of the particle at time  $t$  is  $x(t) = \frac{t}{3}$ . Time is measured in seconds, distance in meters. Let  $a(t)$  denote the arclength distance traveled by the particle along the curve in the first  $t$  seconds.

(a) Set up an integral expression equal to  $a(t)$ . Do NOT attempt to evaluate it.

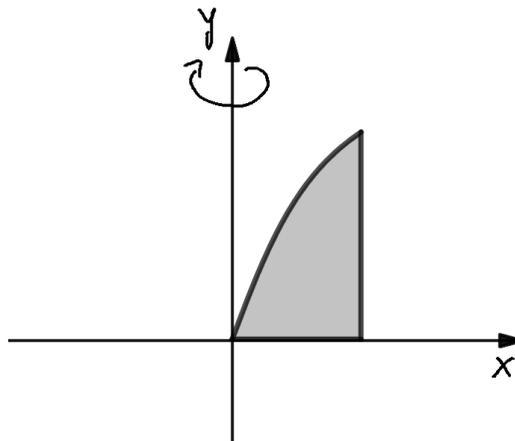
(b) Calculate  $a'(1)$ . Include units.

(c) Use Simpson's Rule with  $n = 4$  subdivisions to approximate the value of  $a(1)$ . Show work, and give your answer correct to 3 decimal places.

6. (10 points) Let  $\mathcal{R}$  be the region in the first quadrant bounded by:

the  $x$ -axis, the curve  $y = 3 \arctan(x)$  and the line  $x = \sqrt{3}$ .

Calculate the volume of the solid of revolution generated by rotating  $\mathcal{R}$  about the  $y$ -axis.



7. (10 points) Find the solution to the differential equation

$$\pi \frac{dy}{dx} = \frac{e^{x-y}}{\sqrt{4 - e^{2x}}}$$

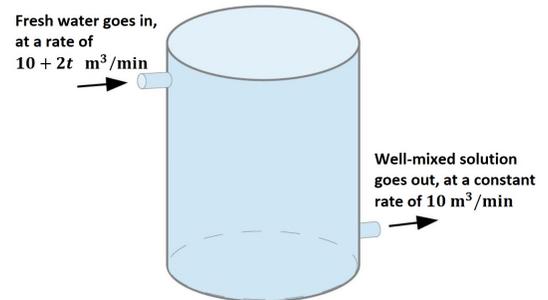
that satisfies the initial condition  $y(0) = 0$ . Give your solution in explicit form,  $y = f(x)$ .

8. (14 points) At time  $t = 0$  minutes a tank holds an initial volume  $V_0 = 100 \text{ m}^3$  of salty water, with an initial amount  $S_0 = 3 \text{ kg}$  of salt dissolved in it.

Fresh water enters the tank at a rate of  $10 + 2t \text{ m}^3$  per minute, where  $t$  is the time in minutes.

The salt always remains uniformly mixed throughout the water solution in the tank, and the solution exits the tank at a constant rate of  $10 \text{ m}^3/\text{min}$ .

- (a) Find a formula for the volume  $V(t)$  of salty water solution in the tank at time  $t$  minutes.



- (b) Set up a differential equation for  $S(t)$ , which is the amount (in kg) of salt in the tank at  $t$  min. Do not solve it yet.

- (c) Solve the differential equation in part (b) to find a formula for  $S(t)$ .

- (d) How much salt is left in the tank after 10 min? Leave your answer in exact form.