

## Answers to Math 124 Winter 2022 Final

- (a) Using L'Hospital's rule or factoring and canceling terms, the limit is 3. (b)-1.5 (c)  $e^{12}$
- (a)  $\frac{dy}{dx} = \frac{(\frac{1}{3}x^{-2/3} + \cos x)(e^x + 1) - (x^{1/3} + \sin x)e^x}{(e^x + 1)^2}$   
 (b)  $\frac{dy}{dx} = \frac{\cos(2^x) \cdot \ln 2 \cdot 2^x}{\sin(2^x)}$   
 (c)  $\frac{dy}{dx} = \sec^2(x^x) \cdot (\ln x + 1) \cdot x^x + \frac{2x}{1+x^4}$
- (a)  $(-3, 2)$  and  $(4, \infty)$  (b) -3,4 (c)  $(-1.4, 3)$  and  $(8, 10)$  (d) -1.4, 3, 10 (e) 18
- (a)  $\tan \theta = \frac{6-x}{x}$ .  
 (b)  $x = 3$   
 (c) Using  $x - 3 \approx -3\left(\theta - \frac{\pi}{4}\right)$ ,  $x - 3 \approx -\frac{3\pi}{64}$ .
- (a)  $\frac{dy}{dx} = \frac{\pi}{2}t \sin\left(\frac{\pi}{2}t\right)$ . When  $t = 1$ , the value is  $\pi/2 > 0$  so  $y$  increases when  $x$  does.  
 (b)  $\frac{d^2y}{dx^2} = \frac{\pi}{2}t \left(\sin\left(\frac{\pi}{2}t\right) + \frac{\pi}{2} \cos\left(\frac{\pi}{2}t\right)\right)$ . When  $t = 1$ , the value is  $\pi/2 > 0$  so the graph is concave up.  
 (c) B
- $-\frac{29.68}{\sqrt{558.25}} \approx -1.256$  feet per second.
- The radius is  $\frac{5}{4+\pi}$ , the width is  $\frac{10}{4+\pi}$ , and the height of the rectangular part is 2.5 (making the total height  $2.5 + \frac{5}{4+\pi}$ )
- (a)  $(1, 0)$  and  $(0, 1)$ .  
 (b)  $y = 0$  on the left.  
 (c) The only critical number is  $x = 0$ . Increasing on  $(-\infty, 0)$  and decreasing on  $(0, \infty)$ .  
 (d) Local maximum at  $(0, 1)$ .  
 (e) Concave up on  $(-\infty, -1)$ , concave down on  $(-1, \infty)$ .

