## HONOR STATEMENT

I affirm that my work upholds the highest standards of honesty and academic integrity at the University of Washington, and that I have neither given nor received any unauthorized assistance on this exam.

Name	Signature
Student ID #	Please circle Section
	AA AB AC
	BA BB BC

	1.	2.	3.	4.	$\sum$
Possible	10	10	15	15	50
Points					

- Please turn off your cell phone and put it away.
- There are 4 problems on 10 pages. Check your copy of the exam for completeness. Note that front **and** back of the pages are printed on.
- You are allowed to use a hand written sheet of paper (8x11 in), back and front.
- The only calculator allowed is Ti-30x IIS
- When applicable, make a labeled sketch of the situation. It will grant you at least 1 point.
- Justify all your answers and show your work for full credit.

Do not open the test until everyone has a copy and the start of the test is announced.

GOOD LUCK!

**Problem 1 (10 points)** Consider the quadratic function  $f(x) = 3x^2 + 9x + 2.75$  with domain  $-\infty \le x \le -\frac{3}{2}$ .

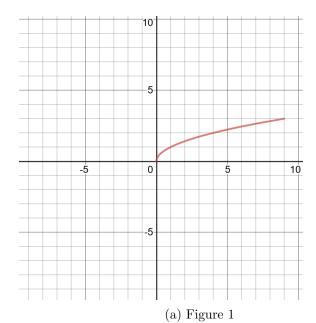
- (a) What is the range of f?
- (b) Find the inverse function  $f^{-1}$  of f.

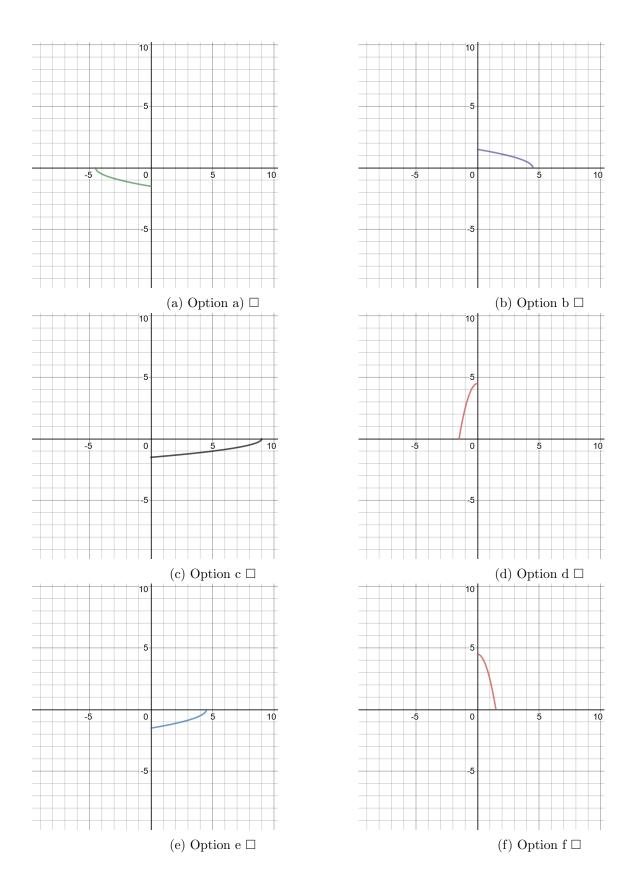
**Problem 2 (10 points)** Consider the function  $f(x) = \sqrt{x}$  on the domain  $0 \le x \le 9$ . A graph of f looks like Figure 1 on page 4. Through shifting, reflecting and dilation this function was altered to  $g(x) = -\frac{1}{2}f(-2x+9)$ .

- (a) Find the domain and the range of g(x).
- (b) Describe the manipulations to the graph we did. Add details by using 'compressed/stretched by factor....', 'reflected about the ....-axis', 'shifted right/left/up/down by .... units':

HORIZONTAL	shift:
	dilation:
	reflection
VERTICAL	reflection:
	dilation:
	shift

(c) Identify the graph of g(x) among the those on page 5.





**Problem 3 (15 points)** The population of City A is growing at a constant rate of 2% each year. In the year 2000, this city had 20,000 inhabitants. The population of City B grows exponentially. In 2010, City B had half as many inhabitants as City A at that time. In 2020, City B had 5,000 inhabitants more than City A. In which year did both cities have the same number of inhabitants?

**Problem 4 (15 points)** While downloading the new season of their favorite TV show, Family Smile notices a slow-down of the download speed. It turns out that the downloaded percentage is a linear-to-linear rational function in time, where time t is measured in minutes. At first, the download was 0%.

After 30 seconds, the download was at 18%.

After 4 minutes, the download was at 60%.

- (a) Where will the download be after 20 long minutes?
- (b) Will it ever finish the download? Explain your answer.

Extra Paper

Extrapaper

Extrapaper