

## Math 120F

### Final Exam (Autumn 1997)-Answers

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1. (a) (i)  $3 + 4h + h^2$ . (ii)  $4 + h$ .  
(b)  $f(g(-1)) = -3/4$ .  $g(f(-1)) = -1$   
(c)  $x = -4 \ln(1.4) = -1.3459$   
(d)  $y = 2^{3x+1} - 5$ .
2. (a)  $A = 15, B = 4, C = 3, D = 215$ . Also,  $C = 3 + 4k$ ,  $k$  an integer is acceptable.  
(b)  $225.6^\circ$ .  
(c)  $t = 3.216, 4.784, 7.216, 0.784$ .
3. (a)  $y = 59000(1.12)^t$ .  
(b) \$92,823  
(c)  $f(t) = 100000e^{0.047t}$ .  
(d) 7.96 years after January 1, 1997.
4. (a)  $x(t) = 3 \cos(\frac{\pi}{2} - \frac{2\pi}{3}t)$ .  $y(t) = 3 \sin(\frac{\pi}{2} - \frac{2\pi}{3}t) + 4$ .  
(b)  $(-2.88, 4.85)$
5. (a)  $x(t) = 61.1t$ .  $y(t) = 91.5t - 16t^2$ .  
(b)  $y = 1.497x - 0.0043x^2$ .  
(c)  $t = 3.8$  seconds.  $(232.6, 116.3)$   
(d) 51.3 ft/sec.
6. (a) Area  $= -2.145y^2 + 30y$ .  
(b) 15 inches by 6.995 inches.
7. (a)  $x(t) = 20 - 5t$ ,  $y(t) = -20 + 2.5t$ .  
(b)  
$$d(x) = \begin{cases} 20 - 2.5t & \text{if } 0 \leq t \leq 4 \\ \sqrt{(20 - 5t)^2 + (-20 + 2.5t)^2} & \text{if } 4 \leq t \leq 8 \end{cases}$$
  
(c)  $t = 2, 6.95$ .