Math 441

Topology

Fall 2012

## Assignment #3: Supplementary Problem

**Problem S1:** Let Y denote the following subset of  $\mathbb{R}^2$ , with the subspace topology:

$$Y = \{(x, y) : x > 0, \ y \ge 0\}.$$

For each of the following subsets of Y, answer each of the following questions (no proofs necessary):

(i) Is it open in Y?

(ii) Is it open in  $\mathbb{R}^2$ ?

(iii) Is it closed in Y?

(iv) Is it closed in  $\mathbb{R}^2$ ?

(a) 
$$A = \{(x, y) \in Y : y > 0\}.$$
  
(b)  $B = \{(x, y) \in Y : y = 0\}.$   
(c)  $C = \{(x, y) \in Y : x = 1\}.$   
(d)  $D = \{(x, y) \in Y : x^2 + y^2 \le 1\}.$   
(e)  $E = \{(1/n, 0) : n \in \mathbb{Z}_+\}.$   
(f)  $F = \{(n, 0) : n \in \mathbb{Z}_+\}.$   
(g)  $G = \{(x, 0) : x \in \mathbb{R}, x > 0\}.$   
(h)  $H = \{(x, 0) : x \in \mathbb{R}, x \ge 1\}.$