

A-1. For each of the functions below, answer the following questions, and *give a complete proof that your answers are correct*.

- Is the function injective?
- Is the function surjective?
- If the function is not surjective, what is its range?

(You may use without proof the following standard fact about the real numbers: for every nonnegative real number x , there exists a unique nonnegative real number \sqrt{x} , called the **square root of x** , such that $(\sqrt{x})^2 = x$.)

(a) $f: \mathbb{R} \rightarrow [0, \infty)$, defined by

$$f(x) = (2 - x)^2.$$

(b) $g: \mathbb{R} \setminus \{1\} \rightarrow \mathbb{R}$, defined by

$$g(x) = \frac{x}{1 - x}.$$