

Do the following problems from [SHE]:

- Exercises 4.4: #38, 43, 45
- Exercises 4.5: #38, 62
- Exercises 4.6: #35, 36
- Exercises 4.8: #20, 32

Prove the following theorem:

- **Theorem A:** Let  $f$  be a function that is continuous on  $[0, \infty)$  and differentiable for all  $x > 0$ . Suppose that  $f'(x)$  satisfies the condition

$$a \leq f'(x) \leq b \text{ for all } x > 0.$$

Then for all  $x > 0$ ,

$$f(0) + ax \leq f(x) \leq f(0) + bx.$$

[Hint: use the Mean Value Theorem.]