## Homework 2 for 509, Homological algebra, Spring 2017 due Wednesday, May 24

**Problem 1.** Let R be a Frobenius algebra over a field k. Show that the global dimension of R is either zero or infinity.

**Problem 2.** Let k be a field of positive characteristic p.

- (1) Show that the group algebra kG for a finite group G is Frobenius (in fact, symmetric).
- (2) Show that the restricted enveloping algebra  $\mathfrak{u}(\mathfrak{gl}_n)$  is Frobenius.