

DEFINITION: A group  $(G, \circ)$  is a set  $G$  together with a binary operation  $\circ$  on  $G$  that satisfies the following three requirements:

- (i) The operation  $\circ$  is associative. That is,  $(a \circ b) \circ c = a \circ (b \circ c)$  for all  $a, b, c \in G$ .
- (ii) There exists an element  $e \in G$  such that  $e \circ a = a$  and  $a \circ e = a$  for all  $a \in G$ .  
The element  $e$  is called the *identity element* of  $G$ .
- (iii) For each element  $a \in G$ , there exists an element  $b \in G$  such that  $a \circ b = e$  and  $b \circ a = e$ .  
The element  $b$  is called the *inverse* of  $a$  and is usually denoted by  $a^{-1}$ .

Assignment 1 (due on Friday, January 18th)

Section 3.4: Problems 2, 6, 7, 8, 10, 15, 25, 26, 31, 40, 44, 45