

NAME _____ TA'S NAME _____

STUDENT ID _____ SECTION _____

Math 124K
Fall 2012

Midterm 2
November 20, 2012

Point totals are indicated in parentheses. You must show your work to receive credit.
Unless indicated otherwise, all answers must be exact.

- (15) 1. Compute the derivative of the following functions. You need not simplify your answer, but your final answers must give the derivative in terms of x .

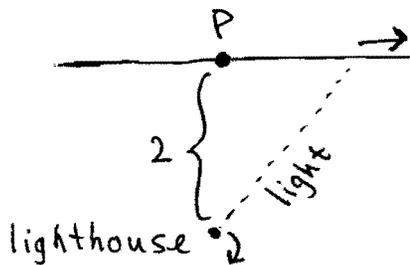
a. $y = [x \sin(x^3)]^{\sqrt{2}}$

b. $y = \tan^{-1}((x^2 + 1)^{\frac{1}{4}})$

c. $y = \ln \left[\left(\frac{1+x}{1+x^2} \right)^x \right]$

- (16) 2. Suppose that a particle is traveling along the curve $4\sqrt{xy+y} + xy^2 - x^2 = -13$.
- (8) a. Find the equation of the tangent line to this curve at the point $(-3, -2)$.
- (4) b. Suppose that the position of the particle at time t is given by $(x(t), y(t))$. Recall then that the speed $s(t)$ of the particle at time t is $s(t) = \sqrt{x'(t)^2 + y'(t)^2}$. If the particle is at $(-3, -2)$ at time $t = 0$ and its speed at this time is 1 with positive horizontal velocity, find $x'(0)$ and $y'(0)$.
- (4) c. With the same assumptions as in part b), use the tangent line approximation to estimate the position of the particle at time $t = 0.1$.

- (12) 3. A lighthouse is located on a small island 2 kilometers away from the nearest point P on a straight shoreline, and its light makes 6 revolutions per minute. How fast is the beam of light moving along the shoreline when it is 1 kilometer from P ? (Remember to give an exact, not a decimal, answer.)



- (12) 4. Let b be a positive constant, and consider the curve C given by the parametric equations

$$\begin{aligned}x(t) &= t^b \cos(\pi t) \\y(t) &= t^b \sin(\pi t)\end{aligned}$$

for t in $(0, 3)$.

- (8) a. Find the slope of the tangent line to the curve at time $t > 0$.
(4) b. For what value of b will the tangent line to the curve at $(-1, 0)$ be $y = 3x + 3$?