| Math 126C | Second Midterm | Winter 2009 |
|--------------|----------------|-------------------|
| Your Name | Your Signature | |
| | | |
| | | |
| Student ID # | | |
| | Lul | ke Chris |
| | Section 11:30 | 12:30 11:30 12:30 |

(circle one)

CA

СВ

CC

CD

| Problem | Total Points | Score |
|---------|--------------|-------|
| 1 | 8 | |
| 2 | 6 | |
| 3 | 14 | |
| 4 | 12 | |
| 5 | 10 | |
| Total | 50 | |

- \bullet This exam is closed book. You may use one $8\frac{1}{2}\times11$ sheet of notes.
- Graphing calculators are not allowed.
- In order to receive credit, you must show your work. Explain why your answers are correct.
- If you use a trial and error (or guess and check) method when a calculus method is available, you will not receive full credit.
- Place a box around YOUR FINAL ANSWER to each question.
- If you need more room, use the backs of the pages and indicate to the reader that you have done so.
- Raise your hand if you have a question.

1 (8 points) Let $\mathbf{r}(t) = (2t-1)\mathbf{i} + t^2\mathbf{j} + 2\sqrt{t}\mathbf{k}$. Find all times t when the tangential component of acceleration is zero.

2 (6 points) Find the equation of the tangent plane of the function $F(x,y) = \frac{3y-2}{5x+7}$ at the point (-1,1).

(14 points) Evaluate the following double integrals.

(a) (7 points)
$$\iint_R xy \sin(x^2y) \, dA, \quad R = [0, 1] \times [0, \pi/2]$$

(b) (7 points) $\iint_D y^2 e^{xy} dA$, $D = \{ (x, y) \mid 0 \le y \le 3, \ 0 \le x \le y \}$

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4 (12 points) You wish to build a rectangular box with no top with volume 6 ft³. The material for the bottom is metal and costs \$3.00 a square foot. The sides are wooden and cost \$2.00 a square foot. Calculate the dimensions of the box with minimum cost. Use the Second Derivative test to verify that your answer is indeed a minimum.

5 (10 points) A table of values is given for a function g(x,y) defined on $R = [0,1] \times [1,4]$. (For example, g(1,4) = 9.4.) Use the table to find a linear approximation to g(x,y) near (0.5,3). Use it to approximate g(0.6,2.8). Carefully explain all your reasoning.

| | | | | | | | 4 |
|------------------|-----|-----|-----|-----|-----|-----|-----|
| 0 | 1 | 1.8 | 2.8 | 3.9 | 5.2 | 6.5 | 8.0 |
| $0 \\ 0.25$ | 1.2 | 1.9 | 2.9 | 4.0 | 5.3 | 6.6 | 8.2 |
| 0.5 | 1.4 | 2.1 | 3.1 | 4.2 | 5.5 | 6.8 | 8.5 |
| 0.75 | 1.6 | 2.2 | 3.3 | 4.5 | 5.8 | 7.0 | 8.9 |
| 0.5 0.75 1 | 1.7 | 2.3 | 3.6 | 4.8 | 6.1 | 7.3 | 9.4 |