Math 125H - Winter 2011 Exam 1 January 27, 2011

Name:		
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Section:		

Student ID Number: _____

PAGE 1	10	
PAGE 2	12	
PAGE 3	15	
PAGE 4	13	
PAGE 5	10	
Total	60	

- There are 7 questions spanning 5 pages. Make sure your exam contains all these questions.
- You are allowed to use a scientific calculator (**no graphing calculators**) and one **hand-written** 8.5 by 11 inch page of notes.
- You must show your work on all problems. The correct answer with no supporting work may result in no credit. Put a box around your FINAL ANSWER for each problem and cross out any work that you don't want to be graded. Give exact answers wherever possible.
- If you need more room, use the backs of the pages and indicate to the grader that you have done so.
- Raise your hand if you have a question.
- Any student found engaging in academic misconduct will receive a score of 0 on this exam.
- You have 80 minutes to complete the exam. Budget your time wisely. SPEND NO MORE THAN 15 MINUTES PER PAGE!

GOOD LUCK!

1. (10 pts) Evaluate the integrals.

(a)
$$\int \frac{e^{2x}}{(e^x+1)^2+1} dx$$

(b)
$$\int \frac{\sin(\ln(x+2))}{(2x+4)\cos^2(\ln(x+2))} dx$$

2. (6 pts) Evaluate $\int_{1}^{3} \left| \frac{x^2 - 4}{x^3} \right| dx$

3. (6 pts) Evaluate the limit by first recognizing an integral that it defines and then evaluate the integral:

$$\lim_{n \to \infty} \sum_{i=1}^{n} \frac{2}{n} \left(1 + \frac{2i}{n} \right) e^{\left(1 + \frac{2i}{n}\right)^2}$$

4. (5 pts) Let $f(x) = \int_{2-x}^{x^2} t e^{\sqrt[3]{t}} dt$. Find f'(1).

5. (10 pts) Let $f(x) = \frac{1}{2}x^2$, $g(x) = x^2$, and $h(x) = ax^2$ for some constant a > 1. A vertical line is drawn at some number x = t and a horizontal line is drawn through the point where x = t intersects g(x). Let A and B be the regions as shown. If the areas of A and B are the same for all values of t, what is the value of a?



6. (13 points)

Consider the region, R, bounded by the curve $y = \sqrt{x+1}$, the x-axis, and between x = 0 and x = 3. A picture of this region is given at right.



- (a) (6 pts) Using both methods (cylindrical shells and cross-sectional slicing), set up two integrals (DO NOT EVALUATE) for the volume of the solid obtained by rotating the region R about the **horizontal line** y = -3.
 - i. Cross-sectional slicing:
 - ii. Cylindrical Shells:
- (b) (7 pts) Find the volume of the solid obtained by rotating the region R about the **vertical** line x = 5. Set up the integral AND evaluate.

7. (10 pts)You are standing on a bridge over a walkway because you want to drop a small water balloon on your math instructor's head.

You are holding out the balloon exactly 65 feet above the ground. Your instructor is 6 feet tall and is walking at a constant speed of 3 feet/sec. Assume the water balloon falls at a constant acceleration of 32 ft/sec². (The picture is not to scale). Let x be the indicated location of the instructor at the instant you release the balloon.

(a) Where should your instructor be located at the instant you **drop** the balloon so that the balloon lands directly on top of his head?



(b) You weren't paying attention and now your instructor is at x = 2 feet away from the location directly below the water balloon. At what initial velocity downward must you throw the balloon, at that instant, in order for it to land on top of his head?