Math 125 - Spring 2007 Exam 1 April 19, 2007

Name:

Section:

Student ID Number: _____

1	12	
2	10	
3	12	
4	12	
5	14	
Total	60	

- You are allowed to use a scientific calculator (**no graphing calculators**) and one **hand-written** 8.5 by 11 inch page of notes. Put your name on your sheet of notes and turn it in with the exam.
- Check that your exam contains all the problems listed above.
- You must show your work on all problems. The correct answer with no supporting work may result in no credit.
- If you need more room, use the backs of the pages and indicate to the grader that you have done so.
- Raise your hand if you have a question.
- Any student found engaging in academic misconduct will receive a score of 0 on this exam.
- You have 50 minutes to complete the exam.

GOOD LUCK!

1. (12 points)

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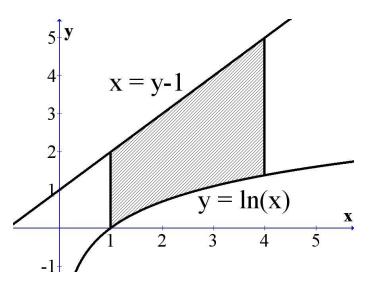
(a) Evaluate
$$\int_{1}^{e} \frac{\sqrt{\ln(x)}}{x} dx$$

(b) If
$$g(x) = \int_0^{\ln(x)} \frac{e^t}{1+t} dt$$
 for $x \ge 1$, find $g'(e)$.

(c) Evaluate:
$$\int_0^3 |3x^2 - 12| dx$$

2. (8 points)

Consider the region, R, bounded by the curves $y = \ln(x)$, x = y - 1, x = 1 and x = 4. A picture of this region is given at right.



(a) Set up an integral tht represents the **area** of the region R. (DO NOT EVALUATE THE INTEGRAL.)

(b) Approximate the **area** of this region using n = 3 approximating rectangles and right endpoints.

3. Evaluate the following integrals:

(a)
$$\int \frac{(1+x)\sqrt{x}}{x} dx$$

(b)
$$\int \frac{\sin(\sqrt[3]{x})}{x^{2/3}} + \cos(x)dx$$

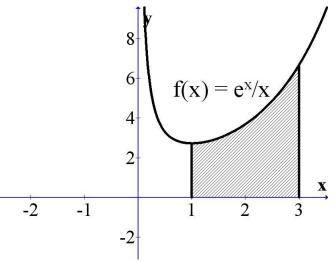
(c)
$$\int x^3 (1+x^2)^{10} dx$$

- 4. Suppose you look out the window of a skyscraper and see someone throw an apple downward. Your window is at a height of 370 feet. The apple passes your window after 3 seconds (from the time it was thrown). The velocity at 3 seconds is -100 feet per second. Assuming that the apple has a constant acceleration of -32 ft/sec², answer the following questions.
 - (a) Give the formula for the position of the apple at time t seconds after being thrown.

(b) Find the velocity at which the apple was thrown and also the height from which it was thrown.

5. Consider the region R bounded by $f(x) = \frac{e^x}{x}$, x = 1, x = 7 and the x-axis. A picture of this region is given at the right.

Consider the region R bounded by $f(x) = \frac{e^x}{x}$, x = 1, x = 7 and the x-axis. A picture of this region is given at the right.



(a) Set up an integral of the form $\int_a bf(x)dx$ that represents the volume of the solid obtained by rotating the region, R, about the line y = -2.

(b) Find the exact volume of the solid obtained by rotating the region, R, about the y-axis.