$\qquad$ Section: $\qquad$

## Math 112

## Group Activity: Rate of Ascent Graphs

A Purple balloon and a Green balloon rise and fall. When we start watching, at $t=0$, both balloons are 30 feet above the ground. Their altitudes at time $t$ minutes are given by functions $P(t)$ and $G(t)$, both measured in feet. The graphs below show the instantaneous rates of ascent of the balloons. That is, the graphs show $P^{\prime}(t)$ and $G^{\prime}(t)$. So, for example, at $t=1$, the rate of ascent of the Green balloon is 15 feet per minute, which means that the Green balloon's altitude is increasing (i.e., the Green balloon is rising) at a rate of 15 feet per minute. Similarly, at $t=1$, the rate of ascent of the Purple balloon is -5 feet per minute, which means that the Purple balloon's altitude is decreasing (i.e., the Purple balloon is falling) at a rate of 5 feet per minute.


1. At $t=0$, the rate graph shows that the Green balloon's rate of ascent is 17.5 and the Purple balloon's rate is -20 . What does that mean about the balloons when we first start observing? Are they rising or falling?
2. During the first 1.5 minutes, the Green balloon's rate graph decreases from 17.5 to 13.75 . What does that mean about the Green balloon? Is it rising or falling? Is it getting faster or slower?
3. The Purple balloon's rate graph is negative during the first 1.5 minutes. What does that mean about the Purple balloon? How does the Purple balloon's rate change during the first 1.5 minutes? Is the balloon getting faster or slower?
4. During the first 1.5 minutes are the balloons getting farther apart or closer together? (Think about whether the balloons are rising or falling during this time period.) Which balloon is higher at $t=1.5$ ?
5. You can't tell their exact altitudes by looking at the rate graphs, but suppose that you are told that at $t=1.5$ minutes, the Green balloon is 54 feet higher than the Purple balloon. Over the next 1.1 minutes, both balloons are rising (how can you tell?) and Green's rate graph is above Purple's rate graph. Are the balloons getting farther apart or closer together from $t=1.5$ to $t=2.6$ minutes?
6. The two rate graphs cross at 2.6 minutes. This means that the balloons are rising at the same rate at that instant. But they do not have the same altitude at $t=2.6$. In fact, since the Green balloon has always been rising faster than the Purple balloon, the two balloons are farther apart at $t=2.6$ than at any previous time, with the Green balloon much higher than the Purple balloon.
Over the next few minutes, beginning at $t=2.6$, both balloons are rising but the Purple balloon's rate graph is above the Green balloon's rate graph. Are the balloons getting farther apart or closer together during the next few minutes beginning at $t=2.6$ ? Explain.
7. Do you agree with the following statement?

During the first four minutes, the balloons are farthest apart at $t=2.6$, when their rate graphs are crossing.
Describe an analogous situation in the context of revenue, cost, and profit.
8. The Green balloon's rate is positive until $t=7$ and then it becomes negative. Describe what you would see the Green balloon do at $t=7$.
9. On the interval from $t=7$ to $t=8$, determine whether each balloon is rising or falling and whether each balloon is getting faster or slower.
10. Again, you can't tell by looking at the rate graphs, but suppose you're told that at $t=8.5$ minutes, the Purple balloon is approximately 32 feet higher than the Green balloon. Describe what happens to the balloons from $t=8.5$ to $t=10$. Are they rising or falling? Getting faster or slower? (BONUS: Do they get closer together or farther apart?)
11. On a separate sheet of paper, draw the basic shapes of the altitude graphs for each balloon, each on a separate set of axes. Don't worry about getting the exact altitudes, just note where each graph is increasing and decreasing and the times at which the balloons change direction (from rising to falling or from falling to rising).

