R problem

Due Friday October 16

Show that if (X, ρ) is a metric space and μ is a Borel measure satisfying

$$\mu(B(x, r)) < \infty \qquad \forall x \in X,\ \forall r > 0,$$

then μ is a Borel regular measure.