

ERRATA TO “ADVANCED CALCULUS” (first two printings)

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The errata listed below were corrected in the third printing. Additional errata found since these corrections were made are in a separate document.

“line $-n$ ” means “line n from the bottom.”

Page 3, line 10: element some \rightarrow element of some

Page 4, Section 1.1, line 3: where points \rightarrow where ordered n -tuples of numbers can represent points

Page 7, line 5: Insert an equal sign after the 3×3 matrix.

Page 8, line 6: point point \rightarrow point

Page 9, Exercise 7b: $c \rightarrow \mathbf{c}$

Page 9, line 7 of §1.2: notation and \rightarrow notation

Page 12, Exercise 8: is a \rightarrow is

Page 13, line 2 after (1.7): $\delta' = \delta \rightarrow \delta' = \delta/\sqrt{n}$

Page 13, line 3 after (1.7): $\delta = \delta'/\sqrt{n} \rightarrow \delta = \delta'$

Page 19, Exercise 2b: Insert “ $f(x, y) =$ ” at the beginning.

Page 19, Exercise 7: Insert “and $q > 0$ ” at the end of the first line.

Page 23, Exercise 4, line 2: 115 \rightarrow 1.15

Page 23, Exercise 5: The f 's should be \mathbf{f} 's.

Page 25, line 3 of proof of Theorem 1.16: all $n \rightarrow$ all k

Page 38, Exercise 4: S and $T \rightarrow S_1$ and S_2

Page 38, Exercise 11b: On the first line, insert “is continuous and” before “satisfies.” At the end, replace “conclude that f must be discontinuous at t_0 ” by “derive a contradiction”.

Page 47, line 2 of proof of Theorem 2.9: $g(a)[f(x) \rightarrow g(a)][f(x)$

Page 54, last line of Example 1: $\partial_1 f \rightarrow \partial_3 f$

Page 60, line 7: $\lim_{t=0} \rightarrow \lim_{t \rightarrow 0}$

Page 60, line -10 : $f(\mathbf{a} + t\mathbf{u} \rightarrow f(\mathbf{a} + t\mathbf{u})$

Page 77, Exercise 4: Replace “ (x, y) , (x, z) , or (y, z) ” by “ (x, y) or (x, z) ” and “all” by “both”.

Page 78, line 4 of Example 1: $2e^{2y} \sin(x^3 + e^{2y}) \rightarrow 2e^{2y} \cos(x^3 + e^{2y})$

Page 82, line 5: The second $\sin^2 \theta$ should be $\cos^2 \theta$.

Page 82, line 6: $\partial^2 u / \partial r / \partial \theta \rightarrow \partial^2 u / \partial r \partial \theta$

Page 84, line 5: Sorry about the formula sticking out into the margin!

Page 89, line 1: $2.63 \rightarrow 2.62$

Page 90, line following (2.66): $k \rightarrow j$

Page 92, line -4: $P_j(\mathbf{th}) \rightarrow P(\mathbf{th})$

Page 94, Exercise 5b: $y^3 \rightarrow y^2$

Page 95, last line of Exercise 10: $\alpha \in S \rightarrow \mathbf{a} \in S$

Page 99, line 11: $12 - 6x \rightarrow 12 - 6x - 8y$

Page 99, lines 15 and -9: alternatively \rightarrow alternately

Page 108, lines -7 to -5: $T \rightarrow L$ (in several places)

Page 109, line -5: Exercises \rightarrow Exercise

Page 110, line 3: to to \rightarrow to

Page 114, lines -9, -8, and -6: $f \rightarrow F$ (5 places)

Page 118, line 3 of Theorem 3.9: $\partial F_i / \partial x_j \rightarrow \partial F_i / \partial y_j$

Page 120, Exercise 9: $3 \rightarrow 6$

Page 122, 2nd line of proof of Theorem 3.11: $\mathbf{f}'(t_0) \neq \mathbf{0} \rightarrow \mathbf{f}'(t_0) \neq \mathbf{0}$

Page 125, Exercise 3, line 1: the set \rightarrow the set $S =$

Page 125, Exercise 6b: $F \rightarrow F_3$

Page 126, line -8: nonegeneracy \rightarrow nondegeneracy

Page 130, line -14: potantial \rightarrow potential

Page 135, caption of Figure 3.8: Insert comma after v^2

Page 137, 4th line of proof of Theorem 3.18: solvablity \rightarrow solvability

Page 139, Exercise 3, line 1: $u = \rightarrow$ Let $u =$

Page 160, Theorem 4.17a: $c_1 f_1 + c_2 f_2 \rightarrow c_1 f_1 + c_2 f_2$

Page 160, Theorem 4.17b: Then f is integrable on S_1 and S_2 if and only if f is integrable on $S_1 \cup S_2$, \rightarrow If f is integrable on S_1 and S_2 then f is integrable on $S_1 \cup S_2$,

Page 163, line -1: is \rightarrow in

Page 167, Exercise 4: A better hint: For any rectangle that does not intersect S , there are slightly smaller rectangles that do not intersect \bar{S} .

Page 168, line 2: $c \rightarrow C$ (two places; to avoid conflict with another use of “ c ” in the same exercise).

Page 174, last line of Example 4: $e^{-3} \rightarrow e^{-1}$

Page 184, line -4: $r^3 \rightarrow r^4$ and $12 \rightarrow 8$.

Page 184, line -2: $\frac{1}{12\pi} \rightarrow \frac{1}{8\pi}$ and $\frac{1}{6} \rightarrow \frac{1}{4}$

Page 184, line -1: $\frac{1}{6} \rightarrow \frac{1}{4}$ and $\frac{16}{9} \rightarrow \frac{8}{3}$

Page 187, Exercise 5: center of mass \rightarrow mass

Page 190, second line after (4.49): $B(r, y_0) \rightarrow B(r, x_0)$

Page 192, last line before exercises: Exercise 7 \rightarrow Exercise 8

- Page 195, display before Corollary 4.57: $b^{p-1} \rightarrow b^{1-p}$
- Page 201, Exercise 2c: $x - 1 \rightarrow 1 - x$
- Page 207, line -10: earlier in this section, \rightarrow in §4.2,
- Page 208, line 2: $\sup \rightarrow \inf$
- Page 208, line 4: $\inf \rightarrow \sup$
- Page 219, line -4: $L'_P(C) \rightarrow L_{P'}(C)$
- Page 227, line 3: regular \rightarrow regular region
- Page 228, Exercise 3: Assume C is positively oriented with respect to the region inside it.
- Page 233, line 7: furface \rightarrow surface
- Page 235, line -9: $S^3 \rightarrow S_3$
- Page 245, line -11: destroyed \rightarrow destroyed
- Page 246, line -5: diaspeared \rightarrow disappeared
- Page 249, lines 4, -11, and -8: $|\eta| \rightarrow |\mathbf{y}|$
- Page 252, Exercise 2, line 2: Delete “potential and” and replace “are” by “is”.
- Page 257, Exercise 7, last line: Replace the formula for $\text{curl } \mathbf{F}$ by $3\mathbf{j} + (z\mathbf{i} - x\mathbf{k})/(x^2 + z^2)^2$.
- Page 258, line 2: f and g are C^1 functions \rightarrow f is C^1 and g is C^2
- Page 263, line 12: $\int_0^z \rightarrow \int_c^z$
- Page 273, line 3: Delete “gives”
- Page 273, line 13: $T \rightarrow \mathbf{T}$
- Page 282, line 2 of proof of Theorem 6.6: $R_k \rightarrow R_{k-1}$
- Page 285, line -1: $\sum_1^k \rightarrow \sum_2^k$
- Page 288, line 13: negligibly \rightarrow negligibly
- Page 289, line 2: $r_n \rightarrow r^n$
- Page 289, line 12: $a_{n+3} \rightarrow a_{N+3}$
- Page 292, line 5: $n[1 - (a_{n+1}/a_n)] > q \rightarrow n[1 - (a_{n+1}/a_n)] < q$
- Page 295, Exercise 23: $x \geq \frac{1}{2} \rightarrow x \geq 1/\sqrt{3}$
- Page 305, Exercise 11: $\sum_0^\infty \rightarrow \sum_1^\infty$
- Page 310, line 1: 7.4 \rightarrow 7.3
- Page 314, Theorem 7.5, line 1: squence \rightarrow sequence
- Page 315, line -14: $(\delta, \infty] \rightarrow [\delta, \infty)$
- Page 317, Example 2, line 1: $x_n \rightarrow x^n$
- Page 317, Example 2, line 6: is it \rightarrow it is
- Page 318, line 2: Weirestrass \rightarrow Weierstrass
- Page 322, Exercise 1: $\sum_1^\infty (-1)^{n-1} n^{-3} \rightarrow \sum_{n=1,3,5,\dots} n^{-3} + 2 \sum_{n=2,6,10,\dots} n^{-3}$
- Page 322, Exercise 5, line 2: $\sum_1^\infty \rightarrow -\sum_1^\infty$
- Page 324, line 1 of Theorem 7.17: $\sum_0^\infty a_n \rightarrow \sum_0^\infty a_n x^n$

Page 329, lines 7 and 8: $-a$ (in exponent) $\rightarrow -\alpha$

Page 332, Exercise 6c: $1 + t \rightarrow 1 + 2t$

Page 338, line -1 : $n \rightarrow k$ (two places)

Page 339, line 2: $n \rightarrow k$ (two places)

Page 341, Exercise 5: $\frac{\log a}{b} \rightarrow \log \frac{a}{b}$

Page 341, Exercise 13: $e^{xt^2} \rightarrow e^{-xt^2}$

Page 346, lines 3, 4, and 5: A factor of 4 is missing.

Page 348, Example 1, line 5: Delete “so”.

Page 357, line 1: $\cos \theta \pm i \sin \theta \rightarrow \cos n\theta \pm i \sin n\theta$

Page 359, line 8: $\frac{\theta e^{-in\theta}}{in} \rightarrow \frac{\theta e^{-in\theta}}{-in}$

Page 362, Exercise 9: integrable \rightarrow piecewise continuous

Page 364, line -5 : $|f(\theta)|^2 \rightarrow |f(\theta)|^2 d\theta$

Page 365, formula (8.14): $\frac{1}{2\pi} \int_{-\pi}^{\pi} \rightarrow \int_{-\pi}^{\pi}$

Page 369, line 7: $\sin(2m-1)\theta \rightarrow (-1)^{m-1} \sin(2m-1)\theta$

Page 376, line -2 : $0 \leq \theta \leq \pi \rightarrow 0 < \theta < \pi$

Page 377, line 4: $(2\pi)^\infty \rightarrow (2\pi)^{-1}$

Page 377, Exercise 6a: $\sum_{-\infty}^{\infty} \rightarrow \sum_{n \neq 0}$

Page 383, equation (8.35): $\exp(-n^2 \pi^2 k t l^2) \rightarrow \exp\left(\frac{-n^2 \pi^2 k t}{l^2}\right)$

Page 386, line 5: the the \rightarrow the

Page 386, formula (8.38): $\sin n\pi c t l \rightarrow \sin \frac{n\pi c t}{l}$

Page 389, Exercise 1, line 3: $\text{cm/sec}^2 \rightarrow \text{cm}^2/\text{sec}$

Page 390, Exercise 3, line 5: insulated \rightarrow constant-temperature

Page 390, Exercise 3, line 6: $\partial_x u(0, t) = \partial_x u(l, t) = 0 \rightarrow u(0, t) = u(l, t) = 0$

Page 390, Exercise 4, line 3: an \rightarrow and

Page 391, Exercise 6b, line -2 : $\sinh c(l-y) \rightarrow \sinh c(L-y)$

Page 399, line -15 : Delete “turns”

Page 399, Exercise 1: $x \rightarrow nx$ (two places)

Page 409, line 5: $(BA)^* \rightarrow (AB)^*$

Page 414, line 4: A35 \rightarrow A.35

Page 415: Formula (A45) should be (A.45)

Page 417, line 6: from $B \rightarrow$ from A

Page 423, line -4 : 4.1 \rightarrow 4.3

Page 425, line -9 : 4.39 \rightarrow 4.37

Page 426, line 3: a the \rightarrow the

Page 426, line -1: $\mathbf{F}(\mathbf{y})| \rightarrow \mathbf{F}(\mathbf{y})\|$

Page 427, line 8: $\|\mathbf{x} - \mathbf{y}| \rightarrow \|\mathbf{x} - \mathbf{y}\|$

Page 434, line -11: $D(S, T) \rightarrow d(S, T)$

Page 439, line -12: $\tilde{F}^1 \rightarrow \tilde{F}_1$

Page 441, Section 1.5, 1(b): $3 \rightarrow 2$ and $-\frac{1}{2} \rightarrow -1$

Page 442, Section 2.5, 4: Delete “ $2yz^2 - 2y^2z^{-3} + 6y$ ”

Page 442, Section 2.6, 3a: $8x^3f_{13} \rightarrow 16x^3f_{13}$

Page 442, Section 2.7, 1: (a) \rightarrow (b)

Page 442, Section 2.7, 2(a): $C = \frac{2}{3} \rightarrow C = 4$

Page 443, Section 2.7, 6: $\frac{3}{2}hk^2 \rightarrow \frac{1}{2}hk^2$

Page 443, Section 2.9, 1: $\frac{1}{4} \rightarrow \frac{1}{2}$

Page 443, Section 2.9, 3: $\min = (308 - 62\sqrt{31})/27$, $\max = 2/3\sqrt{3}$

Page 443, Section 2.9, 15: $(\frac{22}{9}, \frac{4}{3}, \frac{14}{9}) \rightarrow (2, 0, 2)$

Page 443, Section 2.10, 1: $-y^2z^2 = 6xy^3z \rightarrow -y^2z^2 - 6xy^3z$

Page 444, Section 3.3, 2(a): should be $2x - y - z = 3$

Page 444, Section 3.3, 3(a): $\mathbf{f}(u, v)$ should be $(u \cos v, u \sin v, f(u))$

Page 444, Section 3.4, 1(a): $Df \rightarrow D\mathbf{f}$

Page 444, Section 3.4, 2(a): $(v - 2u, 2v - u) \rightarrow (2v - u, v - 2u)$

Page 445, Section 4.3, 3(b): Delete comma after dy .

Page 445, Section 4.3, 5(a): $\frac{9}{8} \rightarrow \frac{17}{8}$

Page 445, Section 4.3, 5(b): $\sin 1 - \sin 2 \rightarrow \sin 2 - \sin 1$

Page 445, Section 4.3, 12: $123 \rightarrow 126$

Page 446, Section 4.4, 15: $\frac{1}{2}\pi^2 \rightarrow \frac{1}{2}\pi^2R^4$.

Page 446, Section 4.5, 2(b): $2 \cos x^4 \rightarrow 2x^{-1} \cos x^5$

Page 446, Section 4.5, 2(c): $4 \rightarrow 2$

Page 446, Section 4.7, 2(d) $\frac{1}{4} \rightarrow \frac{1}{2}$

Page 446, Section 5.1, 4: $\frac{2}{3} \rightarrow \frac{1}{3}$

Page 446, Section 5.1, 5: (c) should be -2π , (d) should be $\frac{9856}{45}$.

Page 447, Section 5.3, 4: The numerator of the coefficients of log and arcsin should be $2\pi ab^2$ rather than b .

Page 447, Section 5.3, 8(c): $\frac{14}{3} \rightarrow 2$

Page 447, Section 5.4, 1(c): The $+$ after \mathbf{i} should be $-$.

Page 447, Section 5.7, 2: $\pi a^2/\sqrt{2} \rightarrow -\pi a^2/\sqrt{2}$

Page 448, Section 6.1, 1(c): $x + x^{-1} \rightarrow 1 + x^{-1}$

Page 448, Section 6.2, 11: Converges \rightarrow Diverges

Page 449, Section 6.4, 18: $|x| = 1 \rightarrow x = 1$

Page 449, Section 7.1, 2: Parts (e), (f), (g) should be (d), (e), (f).

Page 450, Section 7.6, 7: Replace n by k throughout.

Page 451, Section 8.2, 2: Should be $\frac{\pi^2}{3} + 4 \sum_1^{\infty} \frac{(-1)^n}{n^2} [\cos \frac{1}{4}n\pi \cos n\theta + \sin \frac{1}{4}n\pi \sin n\theta]$.

Page 452, Section 8.4, 1(d): $(-1)^{n+1} \rightarrow (-1)^{m+1}$

Page 452, Section 8.4, 2(b): $(-1)^{n+1} \rightarrow (-1)^{m+1}$

Page 452, Section 8.5, 2: $2\pi in\theta \rightarrow in\theta$ (two places) and $(2\pi n)^2 \rightarrow n^2$

Page 452, Section 8.5, 4(a): $2l^2 \rightarrow 2l^2m$