Title: Whyever Iwasawa theory?

Abstract: I hope to explain to the non-expert why the ideas of Iwasawa theory, especially the interplay between arithmetic problems, the complex world and the *p*-adic world, can be used to study a variety of computational and theoretical problems, which otherwise seem inaccessible.