

Math 591 – Tropical Geometry – Final Project

For the final project of this class, you will give a presentation in class and write a paper. The topic can be an exposition of a research paper related to tropical geometry. You are encouraged to think about further questions related to the paper. Only one student can work on a given paper, and projects will be assigned as requested. The project timeline is the following:

Before March 4 Email me with your choice of topic/paper
April 14, 19, 21 Oral presentations (20 minutes each)
April 29, 5pm Final paper due

Below are some suggestions for potential papers (continued on the back page). You are also welcome to find your own – if you like “widgets” try searching for “tropical widget” on <http://arxiv.org/> or <http://www.ams.org/mathscinet/>.

References

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