

## Math 437 – Homework 6

Due 10:15am on Thursday, February 23, 2017

Please indicate any sources you used for a given problem on the solution to that problem. For example, if you worked with another student to get the solution to a problem, please indicate who. You are welcome to work together in small groups, but please try the problems on your own first and write up your own solutions.

### Problem 1.

- (a) Decrypt the following message that was made with a shift cipher:

HFJXFW ZXJI XMNKY HNUMJWX

- (b) Decrypt the following message that was encrypted with a  $2 \times 2$  Hill cipher

TNHSEQWAYUFTHNCU

if you know that the message starts “HI ALICE”

**Problem 2.** (Ch. 6 #18) Prove that  $a \in \mathbb{Z}_m$  will have a multiplicative inverse in  $\mathbb{Z}_m$  if and only if  $\gcd(a, m) = 1$ .

**Problem 3.** Alice and Bob want to share a secret time to meet up and encrypt it using RSA. Bob chooses  $p = 41$  and  $q = 59$  and calculates  $n = p \cdot q = 2419$  and  $m = (p-1)(q-1) = 2320$ .

- (a) Check that  $\gcd(211, m) = 1$  and calculate a find multiplicative inverse for 211 in  $\mathbb{Z}_m$ .
- (b) Bob posts  $n = 2419$ ,  $a = 211$  and Alice sends Bob the encrypted time  $1187 \pmod{n}$ . What is the secret meeting time?