1. (a)
$$f'(x) = \frac{\sqrt{1 + e^{x^2}}\sec^2(x) - \tan(x)\left(\frac{1}{2\sqrt{1 + e^{x^2}}}\right)(2x)e^{x^2}}{1 + e^{x^2}}$$

(b)
$$y' = (\tan x)^{x^2} \cdot (x+1)^{2/3} \left(x^2 \frac{\sec^2(x)}{\tan(x)} + 2x \ln(\tan(x)) + \frac{2}{3(x+1)} \right)$$

(c) (i)
$$g'(t) = \frac{4}{1 + \frac{t}{\ln t}} \cdot \frac{\ln t - 1}{(\ln t)^2}$$

2. (a)
$$4e^4$$
 (b) $-\frac{1}{2}$ (c) $\frac{15}{2}$

3. (a)
$$y-1 = -\frac{16}{7}(x-2)$$
 (b) 1.183 (c) $y'' = -\frac{1326}{343}$ so over-estimate

4. 61.3 mph

5.
$$r = \sqrt[3]{\frac{3000}{4\pi}}$$
 and $h = \frac{1500}{\pi} \cdot \left(\frac{4\pi}{3000}\right)^{\frac{2}{3}}$

- 6. (a) y-intercept y = 0x-intercepts x = 0, 3, 4
 - (b) x = 2 gives a local maximum, x = 3.6 gives a local minimum and x = 0 is neither.
 - (c) Inflection points are (0,0), (1.2,8.7) and (3,0). Concave down if x < 0 or 1.2 < x < 3.
 - (e) Local minimum at about (3.6, -11.2).

Local maximum at (2, 16).



7. (a) c = 4 and d = 1. (b) g'(x) is continuous at x = 1. Note: to get full credit you must use left and right limits, and the definition of the derivative.