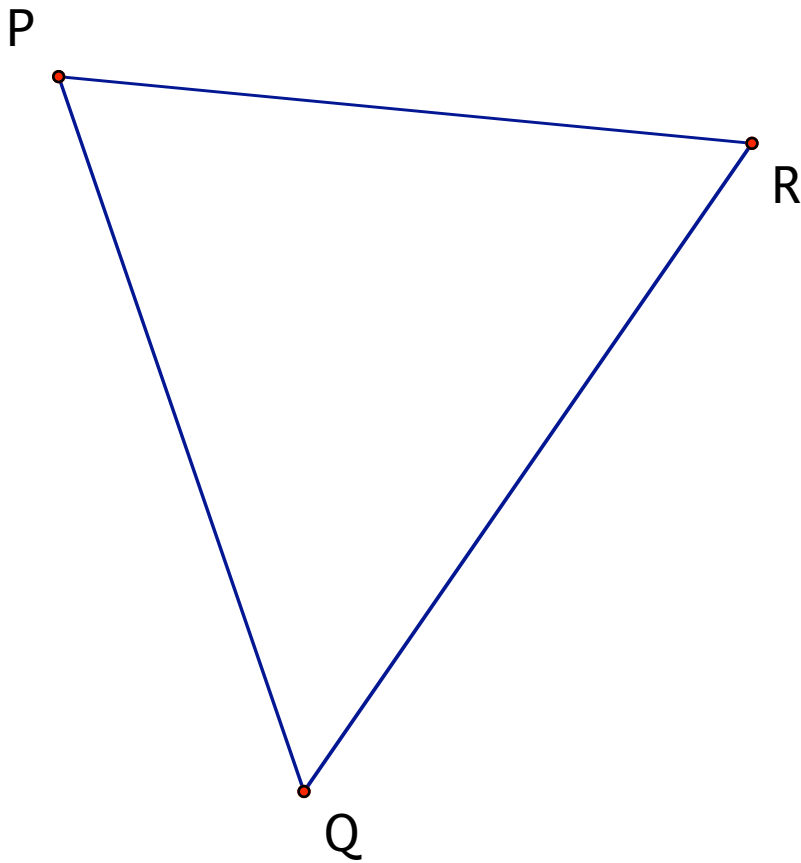


## Construction Portfolio #4

### 27. Altitudes

Construct the 3 altitudes and the orthic triangle of triangle PQR. (The orthic triangle is the triangle formed by the feet of the altitudes.)



### **28. Half Regular Tetrahedron**

Construct a net for half a regular tetrahedron. Specifically, this will be the net for a tetrahedron formed by cutting in two a regular tetrahedron with edge length  $s$ , cutting along one of its planes of symmetry.



**29. Square-based Pyramid (corner vertex)**

Construct a net for a square-based pyramid ABCDE. The square base ABCD has side length  $s$  and the top vertex E is placed so that AE is perpendicular to the plane of ABCD, with  $AE = s$ .



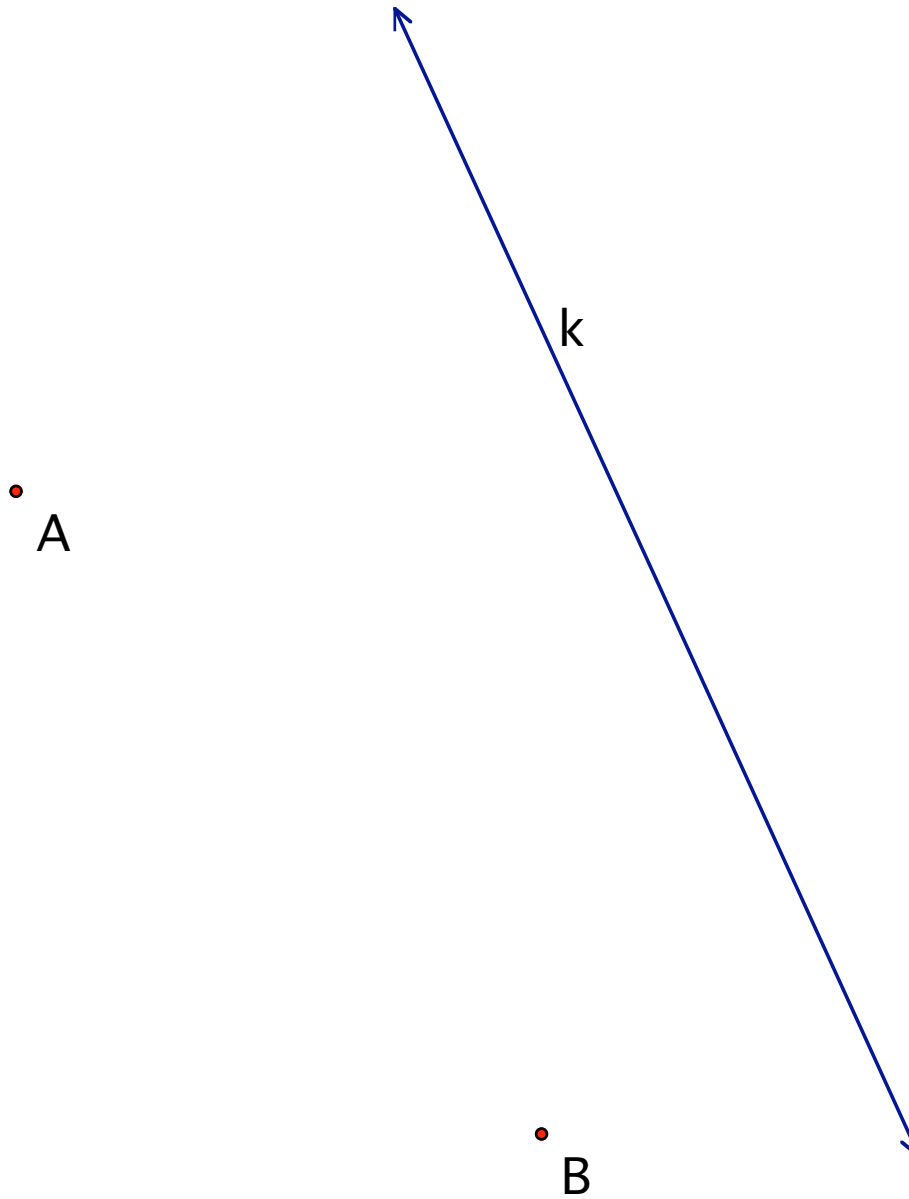
**30. Square-based Pyramid (center vertex)**

Construct a net for a square based pyramid ABCDE formed from one square face ABCD of a cube of side  $s$  and E, the center of the cube.



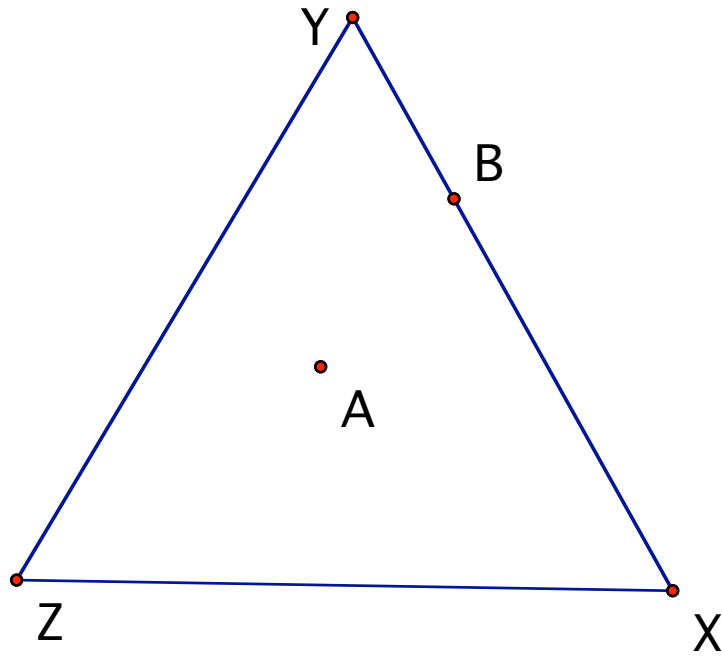
### 31. Light Path

Construct a point  $C$  on line  $k$  so that the path from  $A$  to  $C$  to  $B$  is the shortest possible. Specifically, the sum of lengths  $AC + CB$  should be smaller than for any other point  $C$  on  $k$ . This is the path a beam of light would take from  $A$  to  $B$  if reflected off a mirror  $k$ .



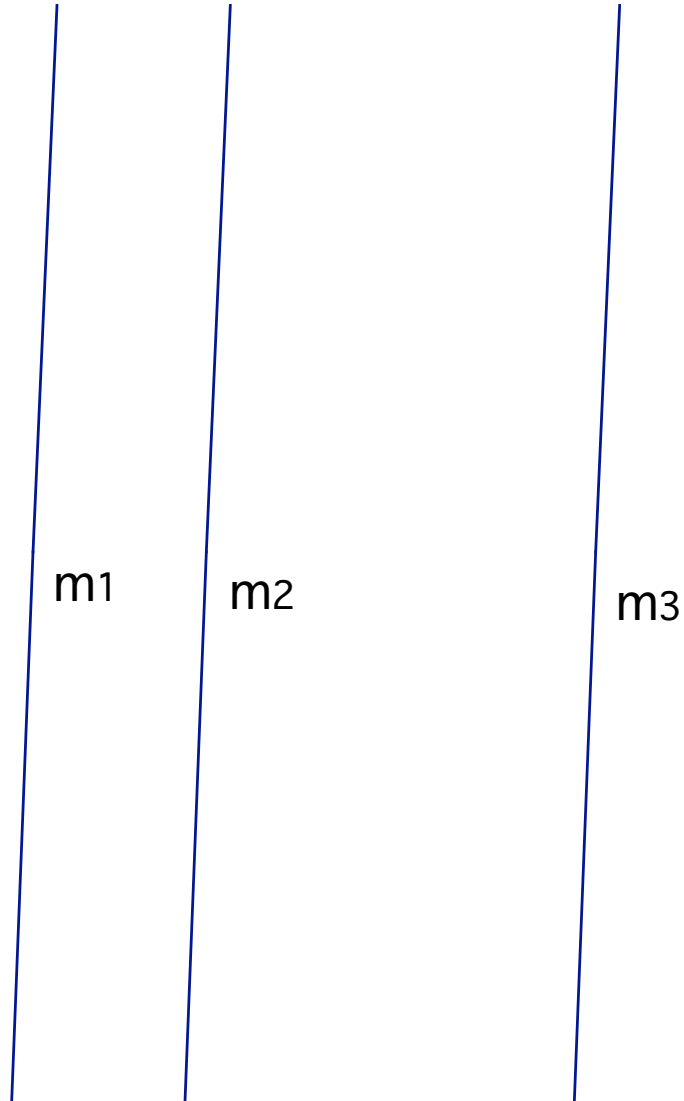
### 32. *Triangular Billiards*

Imagine that  $XYZ$  is a triangular billiard table. Construct the path of a billiard ball that is banked first off side  $XZ$  and then off side  $YZ$  before it reaches  $B$ .



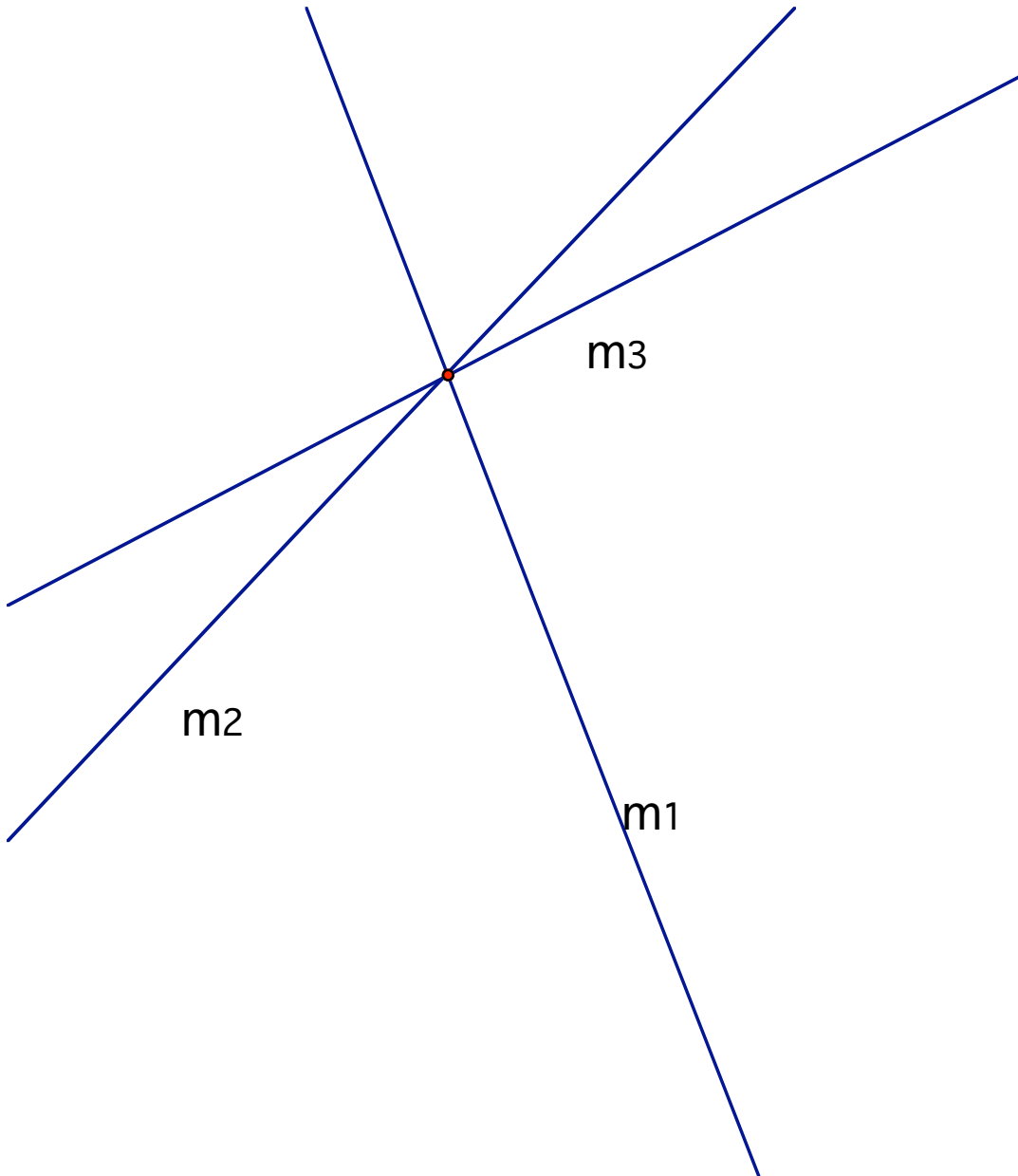
### **33. Triple Line Reflection (parallels)**

Let reflection in parallel lines  $m_1$ ,  $m_2$ ,  $m_3$  be  $M_1$ ,  $M_2$ ,  $M_3$ . Construct a line  $n$  so that reflection in  $n$  is the same transformation as the composition  $M_3 M_2 M_1$ .



### 34. Triple Line Reflection (concurrent)

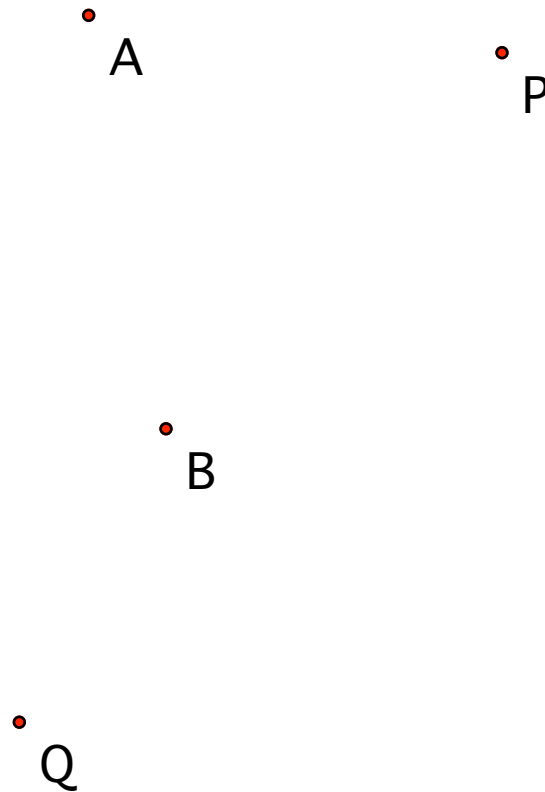
Let reflection in concurrent lines  $m_1$ ,  $m_2$ ,  $m_3$  be  $M_1$ ,  $M_2$ ,  $M_3$ . Construct a line  $n$  so that reflection in  $n$  is the same transformation as the composition  $M_3 M_2 M_1$ .





**35. Composition of two point symmetries**

Given the points A and B, let  $H_A$  and  $H_B$  denote the point reflections with centers A and B. Let S be the composition  $H_B H_A$ . Construct points  $P' = S(P)$  and  $Q' = S(Q)$ .



### 36. Barycentric Coordinates

In this triangle, construct the point P with barycentric coordinates  $1/3, 1/6, 1/2$ . Also, construct the point Q with barycentric coordinates  $x, y, z$ , where the segment EF has length 1.

