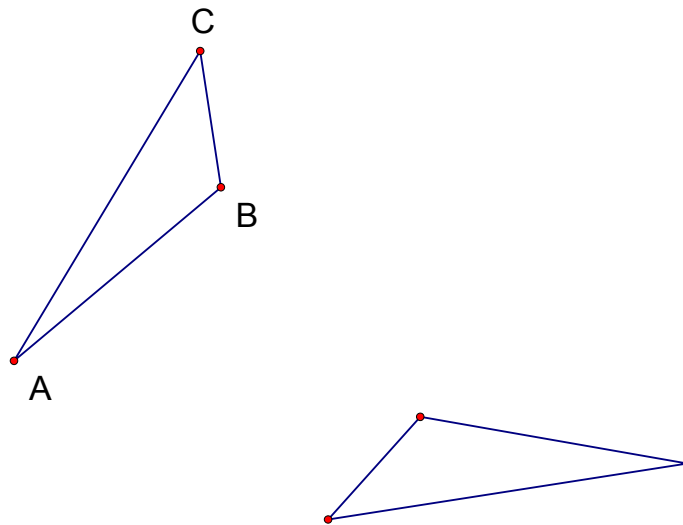


## Construction Portfolio #5

### 37. Center of a Rotation

Construct the center of the rotation that takes triangle ABC to the other triangle (note that this was a problem on Quiz 2 without the information that the isometry is a rotation).



### 38. Center of a Product of Rotations

Given the points A and B below; let S be rotation with center A by 60 degrees and let T be rotation with center B by 180 degrees.

- a) Construct the center C of the rotation  $U = ST$ . Write down the angle of rotation.
- b) Construct the center D of the rotation  $V = TS$ . Write down the angle of rotation.

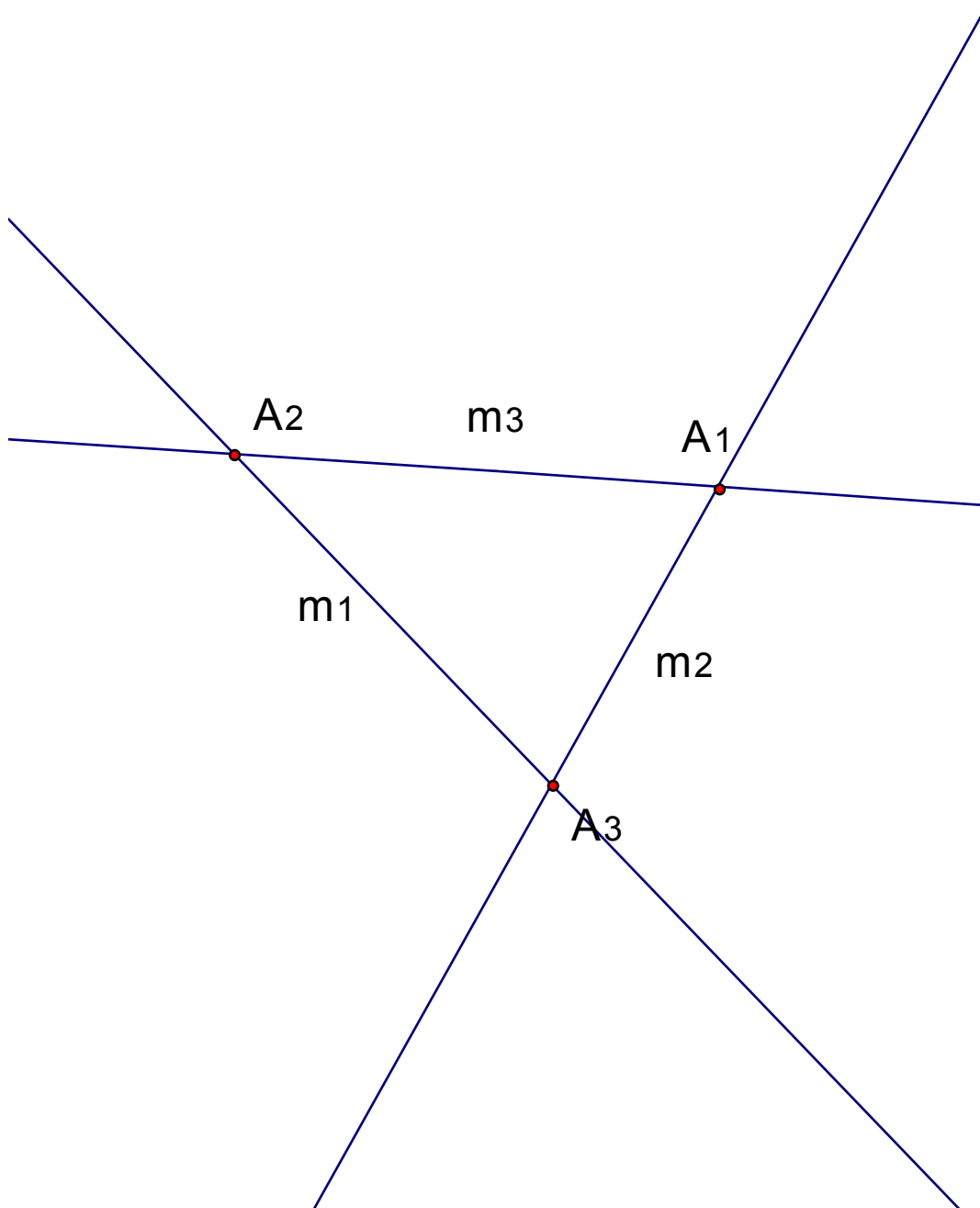
•  
A

•  
B

### 39. Glide Reflection as product of 3 Line Reflections

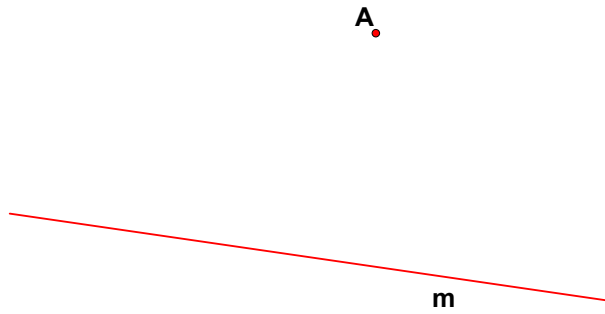
Let  $M_1, M_2, M_3$  be line reflections in the lines  $m_1, m_2, m_3$  below. Let  $N = M_1 M_2 M_3$  and let  $P = M_3 M_2 M_1$ .

- Construct the invariant (special) line of the glide reflection  $N$  and also a glide vector  $XY$ .
- Construct the invariant (special) line of the glide reflection  $P$  and also a glide vector  $UV$ . Question to Ponder: How are  $N$  and  $P$  related?



#### 40. Product of a Rotation and a Line Reflection

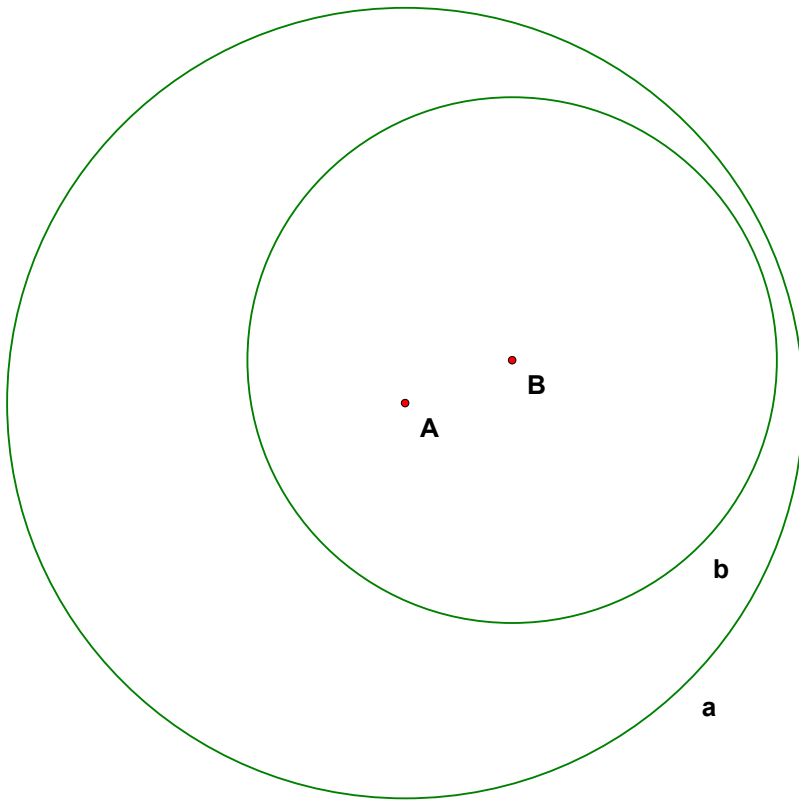
Let  $E$  be rotation with center  $A$  and angle 90 degrees and let  $M$  be reflection in line  $m$ . Construct the geometric defining data of  $ME$ .



### 41. Centers of Dilation

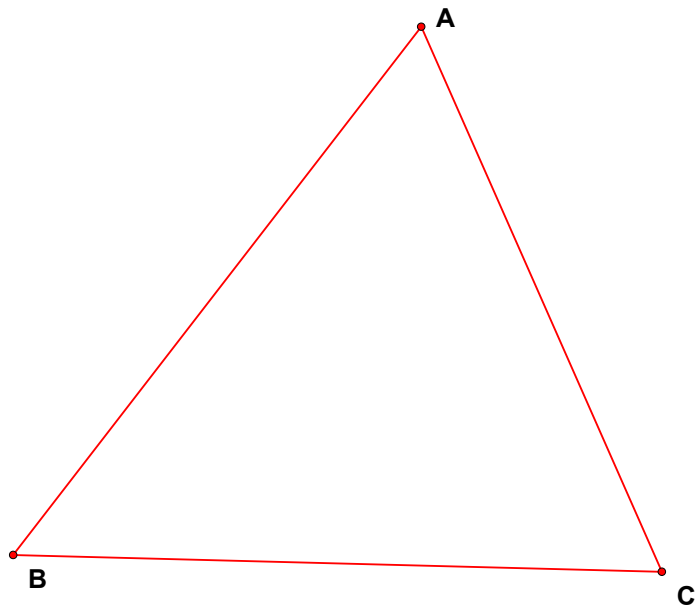
Construct two points P and N so that P is the center of a dilation that takes circle a to circle b with positive ratio and N is the center of a dilation that takes circle a to circle b with negative ratio.

Question to Ponder: The ratio of the radii of a and b is 1.5. How are the distances among the points A, B, P, N related? If  $AB = d$ , what are the other distances?



## 42. Nine-Point Circle and Euler Line

- Construct the Circumcircle of triangle ABC with circumcenter O.
- Construct the Orthocenter H of triangle ABC.
- Construct the Centroid G of triangle ABC.
- Construct the Nine-Point Circle of triangle ABC with center B, with the 9 special points indicated.
- Construct the Euler line of triangle ABC.



### 43. Image of an Isometry

In the figure are given congruent quadrilaterals  $ABCD$  and  $A'B'C'D'$ . There is a unique isometry  $T$  that takes  $ABCD$  to  $A'B'C'D'$ , i.e.,  $A'B'C'D'$  is  $T(ABCD)$ , the image of  $ABCD$ .

Construct the quadrilateral  $A''B''C''D''$  that is  $T(A'B'C'D')$ , the  $T$  image of  $A'B'C'D'$ .

