

Name: \_\_\_\_\_

## Test Prep — 15.2 (General Regions in terms of $x$ or $y$ ) — Math 126

### Participation:

- +1: show written work from 15.2 homework; +1: participate in this test prep

Ch. 15 Problem Solving Template Review (same as 15.1)

- STEP 1 : Integrand? Write  $\iint_D ?? dA$
- STEP 2 : Draw the region,  $D$ , on the  $xy$ -plane.
- STEP 3 : Bounds — describe the region (**what today is about!**)
- STEP 4 : Evaluate.

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**Notes on describing the region:** The SAME advice and tools from Math 125.

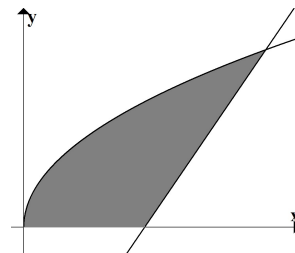
- Draw the region first. Everything comes from the picture.
- For the order  $\int \int ?? dy dx$ , we are fixing  $x$  and describing  $y$  in terms of  $x$  (i.e. top/bottom).  
**One curve on top and one on bottom** for the entire region... use  $dy dx$ .  
Meaning label  $x$  on the  $x$ -axis and label all curves in terms of  $x$ .
- For the order  $\int \int ?? dx dy$ , we are fixing  $y$  and describing  $x$  in terms of  $y$  (i.e. left/right).  
**One curve on left and one on right** for the entire region... use  $dx dy$ .  
Meaning label  $y$  on the  $y$ -axis and label all curves in terms of  $y$ .

*Most mistakes in this section are not calculus mistakes — they are region mistakes.*

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### Winter 2016 - Exam 2 - Dr. Loveless (general region)

- 3(b) (7 pts) Let  $R$  be the region in the first quadrant of the  $xy$ -plane bounded by  $y = x - 2$  and  $y^2 = x$  (as shown). Set up the double integral  $\iint_R 2y dA$  both ways. First in terms of  $y$  (easier), then in terms of  $x$  (requires splitting the region into two parts).



For all below, try to set it up, then compare with classmates and your TA. All solutions are in the exam archive.

**Spring 2014 - Exam 2 - Dr. Loveless**

3(a) Let  $D$  be the region bounded by  $y = x^2$  and  $y = 2x$ . Evaluate:  $\iint_D (x + y) dA$

**Winter 2016 - Exam 2 - Dr. Loveless**

3(b) Let  $D$  be the region bounded by  $y = x$ ,  $y = 0$ , and  $x = 2$ . Evaluate:  $\iint_D x dA$

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**Spring 2013 - Exam 2 - Dr. Loveless (reversing order)**

3(a) Evaluate the integral by reversing the order of integration:  $\int_0^4 \int_{y/2}^2 f(x, y) dx dy$ .  
(*The goal is to draw the region, then relabel.*)

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Please, please ask if you are having trouble drawing or labeling. These skills are not just important for this class — they show up in almost every math and science course you take.