## Math 124 C - Winter 2010

Exam I Hints and Answers - Version Alpha

1. (3 points each)
(a) ANSWER: -6
(b) ANSWER: $-\infty$
(c) ANSWER: 1
(d) HINT: Investigate the limits from the left and the right. They are not equal. ANSWER: does not exist
2. (3 points each)
(a) ANSWER: $\frac{d y}{d x}=x^{3} e^{x}+e^{x} \cdot 3 x^{2}$
(b) ANSWER: $f^{\prime}(x)=\frac{\left(x^{2}+x-2\right) \cdot e^{10 x} \cdot 10-e^{10 x} \cdot(2 x+1)}{\left(x^{2}+x-2\right)^{2}}$
(c) ANSWER: $\frac{d y}{d x}=4 \cos x+x^{-2}-15 x^{-4}$
(d) ANSWER: $g^{\prime}(x)=\left[\sec ^{2}\left(x^{2}\right)\right] \cdot 2 x$
3. (8 points)

4. (a) (4 points) ANSWERS: The line $x=-1$ is a vertical asymptote. The line $y=2$ is a horizontal aslymptote.
(b) (6 points) ANSWER: $f^{\prime}(x)=\frac{2}{(x+1)^{2}}$
5. (8 points) HINT: The line tangent to $g(x)$ at $x=a$ has slope $g^{\prime}(a)=2 a$. On the other hand, this line goes through the two points $(a, g(a))=\left(a, a^{2}+6\right)$ and the point $(0,-2)$. So, another expression for the slope of the same line is $\frac{a^{2}+6-0}{a+2}$. Set $2 a$ equal to $\frac{a^{2}+6}{a+2}$ and solve for $a$.
ANSWER: $a=-2 \pm \sqrt{10}$
