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Math 111
Group Activity: Maximizing Profit Three Ways
You work for Tasty Tours, organizing tours of a local winery. In order to make your tour competitive with other companies, you offer price breaks for larger groups. The following table gives the price per person (in dollars), the total revenue (in dollars), and the marginal revenue (in dollars per person) for different values of $q$ (in number of people).

| $q$ | 10 | 20 | 25 | 30 | 35 | 40 | 60 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $p$ | 26 | 22 | 20 | 18 | 16 | 14 | 6 |
| $T R$ | 260 | 440 | 500 | 540 | 560 | 560 | 360 |
| $M R$ | 21.60 | 13.60 | 9.60 | 5.60 | 1.60 | -2.40 | -18.40 |

Your costs come from the winery and caterer, who charge you $\$ 8$ per person. You also have fixed costs in the amount of $\$ F C$.

1. (a) The value of marginal cost is the same for all quantities. What is the marginal cost? Include units.
(b) Recall how marginal revenue and marginal cost determine the quantity that maximizes profit and use the above table to estimate the number of people that yields maximum profit.
2. The following is the graph of total revenue.

(a) Sketch the graph of variable cost on the axes above.
(b) Use the graphs of $T R$ and $V C$ to approximate the number of people that yields maximum profit.
3. (a) The price per person $p$ is a linear function of quantity $q$. Using the information given in the table, find this linear function.
(b) You now have a formula for the price of a tour per person for a group of $q$ people. Use this to find the formula for your total revenue: $T R(q)$. What are the units associated with $q$ in your formula? With $T R(q)$ ?
(c) Recall that $M R(q)=\frac{T R(q+1)-T R(q)}{1}$ and find a linear formula for $M R(q)$. What are the units associated with $q$ in your formula? With $\operatorname{MR}(q)$ ?
(d) Use the formulas for $M R$ and $M C$ to determine the number of people that yields maximum profit.
4. You used three different methods to find the quantity that maximizes profit: using a table of values of $M R$, graphs of $T R$ and $V C$, and using formulas for $M R$ and $M C$. The three methods should have yielded similar results. Discuss the advantages and disadvantages of using each method.
